

B&K mixing and CP asymmetries in SUSY at NLO

M.Ciuchini, E.Franco, D.Guadagnoli, V.Lubicz, V.P., L.Silvestrini

We derive bounds on the squark mass splittings comparing the full NLO computation of gluino-mediated contributions to $\Delta B=2$ and $\Delta S=2$ processes with the measured values of

$$\Delta M_K$$

$$\epsilon_K$$

$$a_{J/\psi K_s}$$

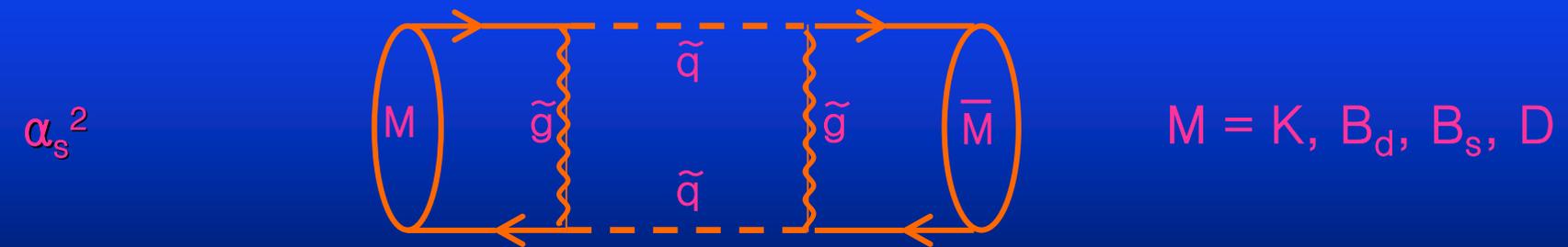
$$\Delta M_d$$

$$\Delta M_s$$

analysis in progress...

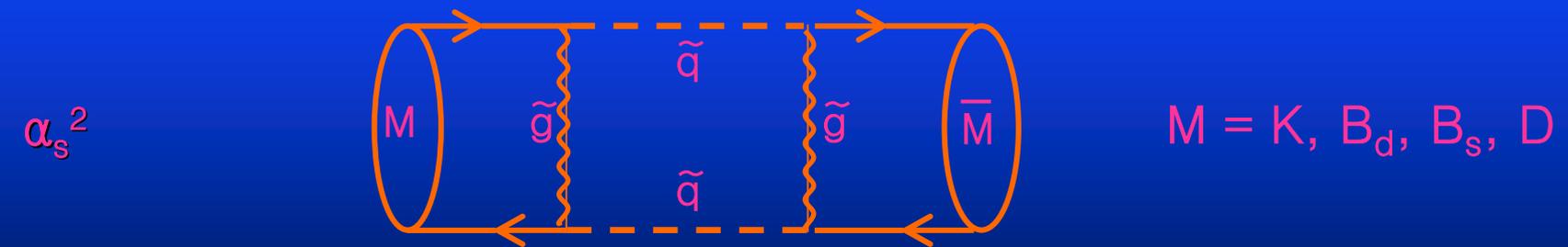
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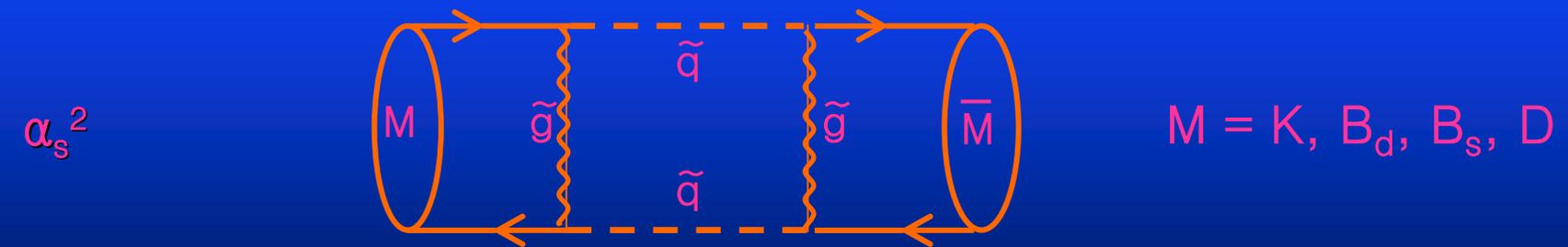
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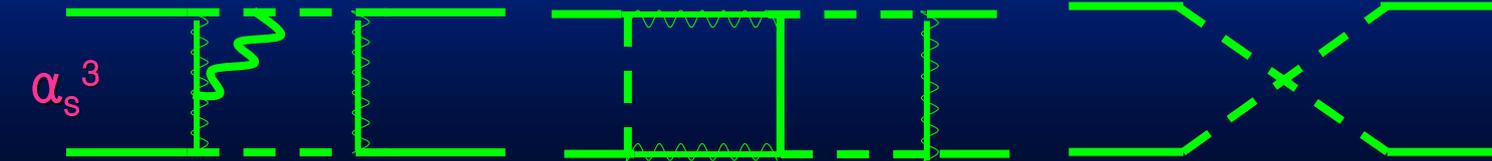
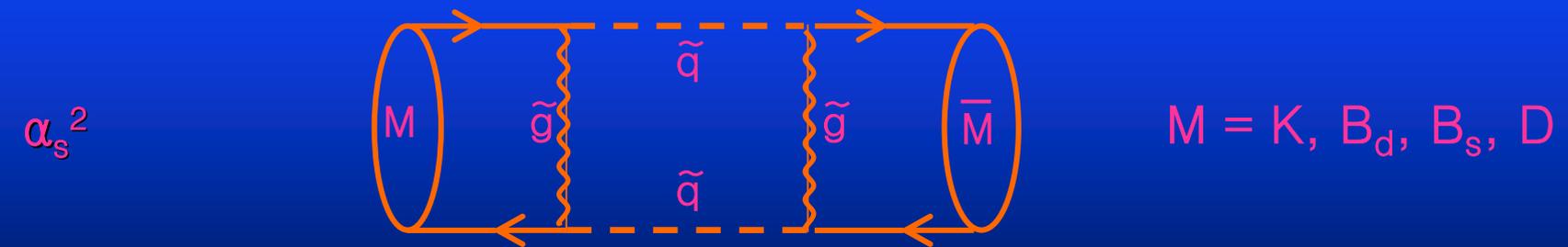
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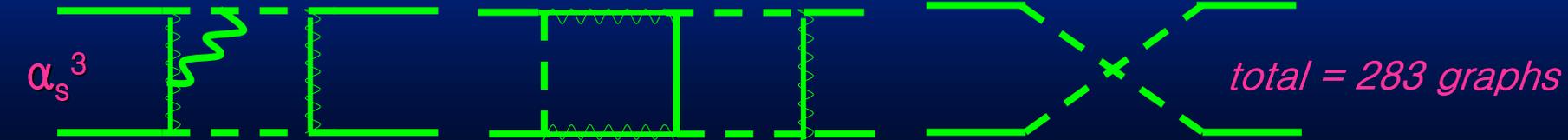
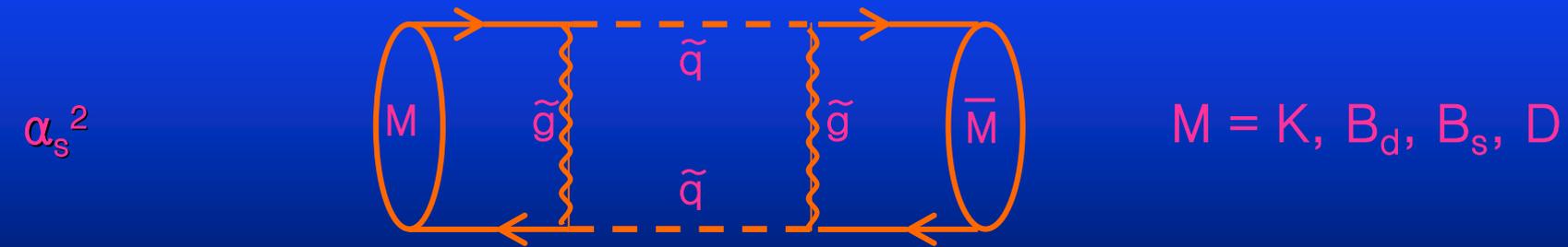
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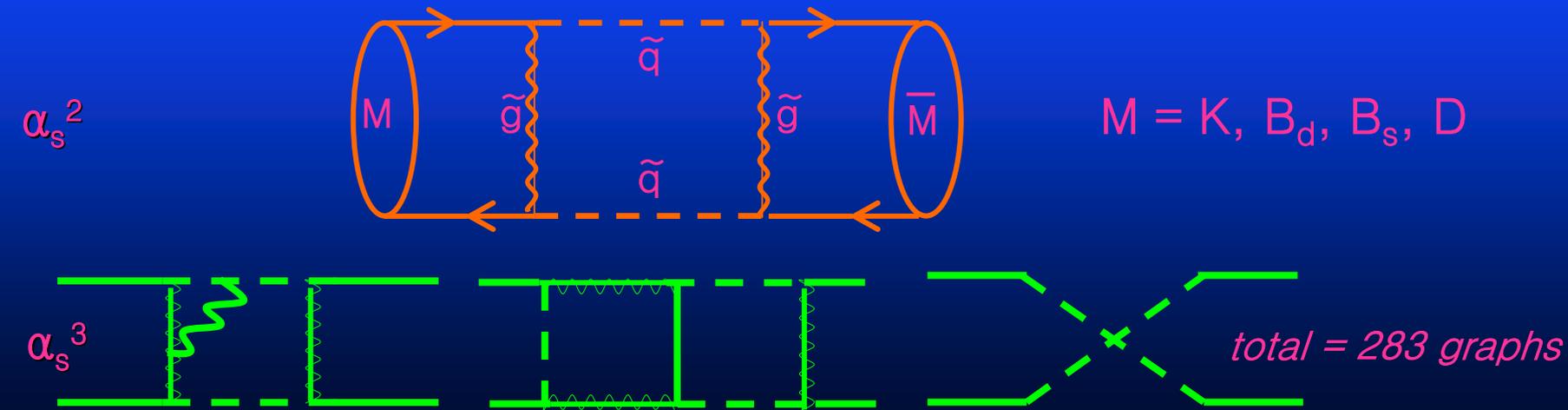
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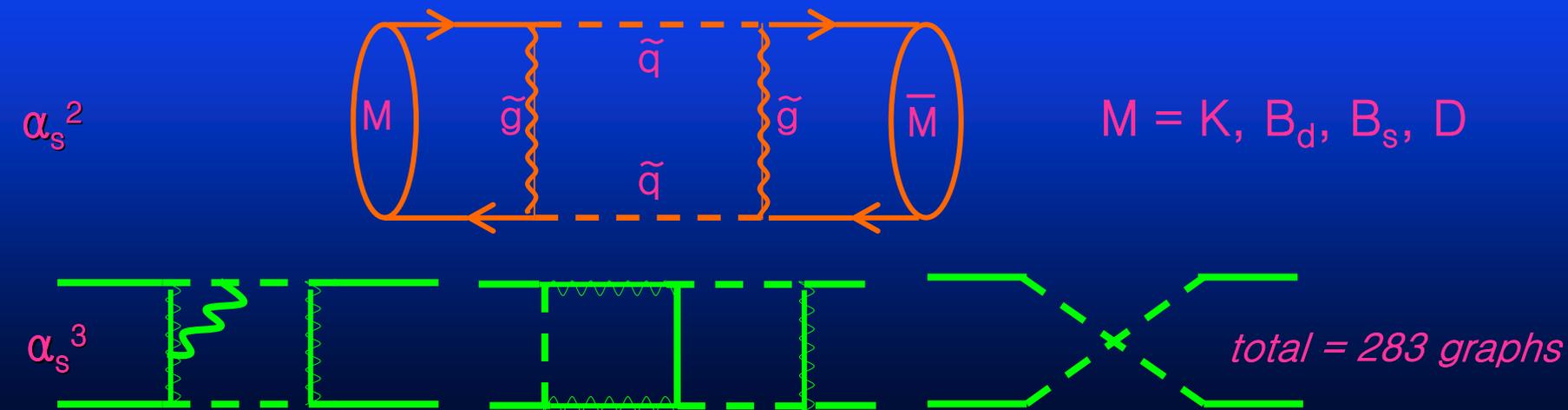
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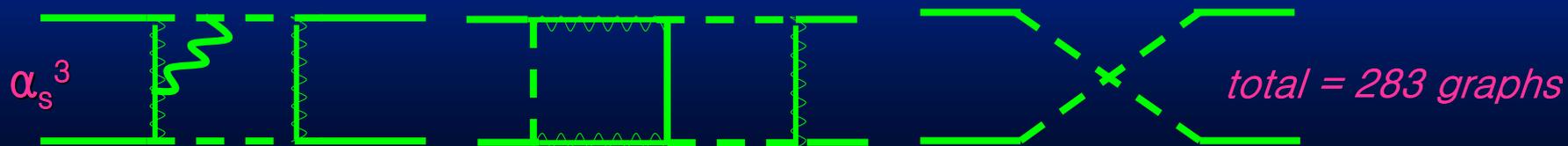
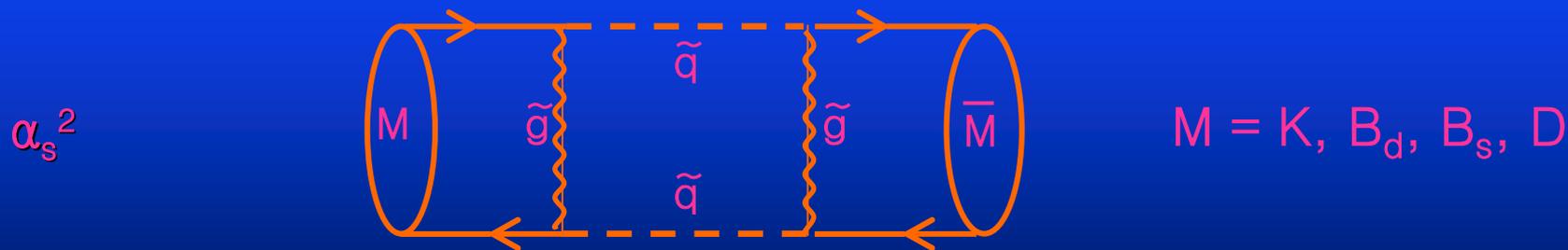
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And what is (still) missing

- global analysis including also charginos, neutralinos, charged Higgs exchange
- unquenched $B_{3,4,5}$ parameters

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The basic problem

It is an unexpected experimental fact that in charged current weak interactions the mass eigenstates are mixed.

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we use FCNC and CP violating processes to constrain the huge SUSY parameter space

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focus on SUSY squark sector

Squared mass matrix for the squarks $(\tilde{d}_L, \tilde{s}_L, \tilde{b}_L, \tilde{d}_R^*, \tilde{s}_R^*, \tilde{b}_R^*)$ in the basis where
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- *White terms are flavour diagonal and come from a flavour blind $\mathcal{L}_{\text{soft}}$*
- *Orange terms are driven by radiative corrections [c_i running coeff. contain $\log(M_{\text{NP}}/M_W)$] and are governed by $V=V_{\text{CKM}} \rightarrow$ FCNC in the strong interactions $q\bar{q}g$*

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Every block is 3x3 in flavour space

$$\begin{pmatrix} m_1^2 & \Delta^{12} & \Delta^{13} \\ \Delta^{21} & m_2^2 & \Delta^{23} \\ \Delta^{31} & \Delta^{32} & m_3^2 \end{pmatrix}_{\text{LR}}$$

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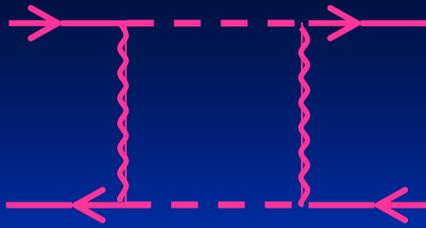
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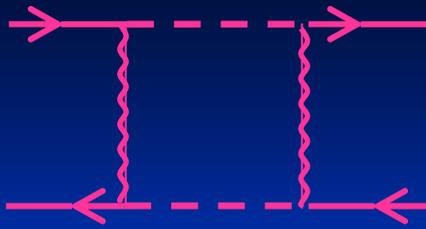
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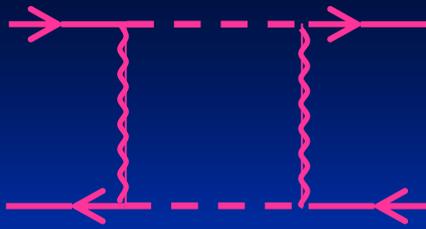
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In order to properly account for the scheme and scale dependence in the physical result *2 loop diagrams are needed*

Low energy part

Integrating out squarks and gluinos gives the operators (SUSY basis)

$$Q_1 = \bar{d}_L^\alpha \gamma_\mu b_L^\alpha \bar{d}_L^\beta \gamma_\mu b_L^\beta$$

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$$\tilde{Q}_{1,2,3} = Q_{1,2,3} (L \leftrightarrow R)$$

The matrix elements of the operators between the mesons M are given in the Vacuum Insertion Approximation (VIA) as functions of the quark and the meson masses and decay constant.

The effect of non-factorizable corrections is contained in the B parameters

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important: $Q_{2,3,4,5}$ can be enhanced with respect to Q_1 by $m_M^2/(m_{q_1} + m_{q_2})^2$

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While working in d-dim define $EO = Q_1^{\alpha\alpha\beta\beta} - Q_1^{\alpha\beta\beta\alpha} = O(\epsilon)$.
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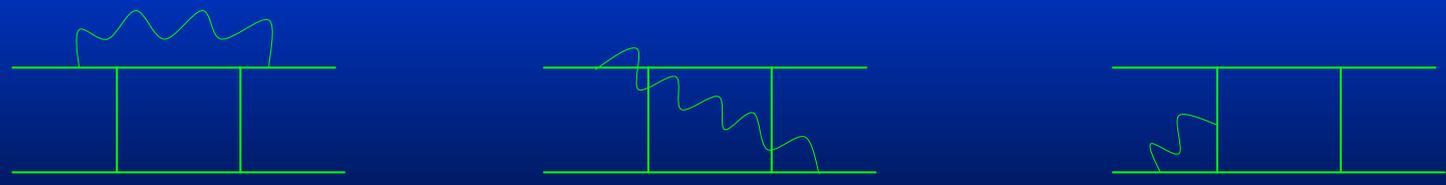
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Solutions

- avoid IR div: we gave mass to the gluon (done NDR and DRED)
- do the matching in d-dim keeping also EO's (checked in DRED where EO's arise when a $g_{\mu\nu}$ in 4-dim from γ algebra meets a $g_{\mu\nu}$ in d-dim from impulses)

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But you are assuming that

- ↓ the off diagonal entries in M_D are small quantities
- ↓ the diagonal entries are nearly degenerate
- ↓ no interference effects occur

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CASE 3

You compute the Wilson coefficients of whatever model that extends the SM adding new heavy particles.

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calculated NLO in terms of
 $m_{\tilde{q}}, m_{\tilde{g}}, \delta$'s

$\bar{B}_s\bar{B}_s$ system $\rightarrow \delta_{23}^d$

interesting but only bounded:

– The SM amplitude is real

$$- \left(\frac{\Delta m_d}{\Delta m_s} \right)_{\text{SM}} \sim \left(\frac{\Delta m_d}{\Delta m_s} \right)_{\text{MSSM}}$$

The method

$$\overline{\langle M | \mathcal{H}^{\Delta S=2} | M \rangle} = \text{Re } A_{\text{SM}} + i \text{Im } A_{\text{SM}} + A_{\text{SUSY}} \text{Re}(\delta_{ij}^d)^2_{AB} + i A_{\text{SUSY}} \text{Im}(\delta_{ij}^d)^2_{AB}$$

The constraints are obtained imposing that the sum of SUSY contributions is proportional to a single δ and the SM contribution reproduce the measured value of the observable. The d 's appear quadratically in the Wilson coefficients in the combinations

$$\delta_{LL}^2 \quad \delta_{RL}^2 \quad \delta_{LL}\delta_{RR} \quad \delta_{LR}\delta_{RL} \quad \delta_{RR}^2 \quad \delta_{LR}^2$$

the mixed products are bounded setting $\delta_{ij} = \delta_{kl}$

This is the main limit of the analysis \rightarrow interference effects possible
order of magnitude bounds

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The parameters x_i are extracted from flat distribution in $[x_i - \sigma_i, x_i + \sigma_i]$

The average observables O are calculated with the weighting factor

$$e^{-\frac{(O(x_i) - O_{\text{exp}})^2}{\sigma_{\text{exp}}^2}}$$

[if $\sigma_{\text{exp}} \ll$, not efficient \rightarrow we solve in the less constrained parameter]

Main input parameters used in the preliminary analysis

$$\sin 2\beta = 0.726 \pm 0.037$$
$$\Delta m_d \text{ (ps}^{-1}\text{)} = 0.502 \pm 0.006$$

CKM parameters from the UTfit (www.utfit.org)
only measures New Physics free

$$\bar{\rho} = 0.21 \pm 0.10$$
$$\bar{\eta} = 0.36 \pm 0.06$$
$$\lambda_c = 0.2258 \pm 0.0014$$
$$V_{cb} = 0.0416 \pm 0.0007$$

B-parameters

from [hep-lat/0110091](https://arxiv.org/abs/hep-lat/0110091) in RI-MOM

$$B_1(m_b) = 0.87(4)^{+5}_{-4}$$

$$B_2(m_b) = 0.82(3)(4)$$

$$B_3(m_b) = 1.02(6)(9)$$

$$B_4(m_b) = 1.16(3)^{+5}_{-7}$$

$$B_5(m_b) = 1.91(4)^{+22}_{-7}$$

The plots shown here are at fixed values of the squark and gluino masses:

$$m_{\tilde{q}} = m_{\tilde{g}} = 350 \text{ GeV}$$
$$x = m_{\tilde{g}}/m_{\tilde{q}} = 1$$

How do the constraints on the δ 's vary with x and $m_{\tilde{g},\tilde{q}}$?

- The results of the analysis are reliable for $x \leq \mathcal{O}(1)$. However

$x > 1$ disfavoured by the evolution from M_{PL} to M_{W} : $x_{\text{W}} = \frac{9 x_{\text{PL}}}{1 + 7 x_{\text{PL}}}$
 $x \ll 1$ only in specific models

- If $m_{\tilde{q},\tilde{g}}$ or $x \rightarrow \infty$, the bounds on the δ 's become loose

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The constraints on the δ 's don't solve to the flavour problem:

very high scale for new physics

$m_{\tilde{g},\tilde{q}} \gg$ and loose δ 's

or flavour symmetries + new physics at lower scale

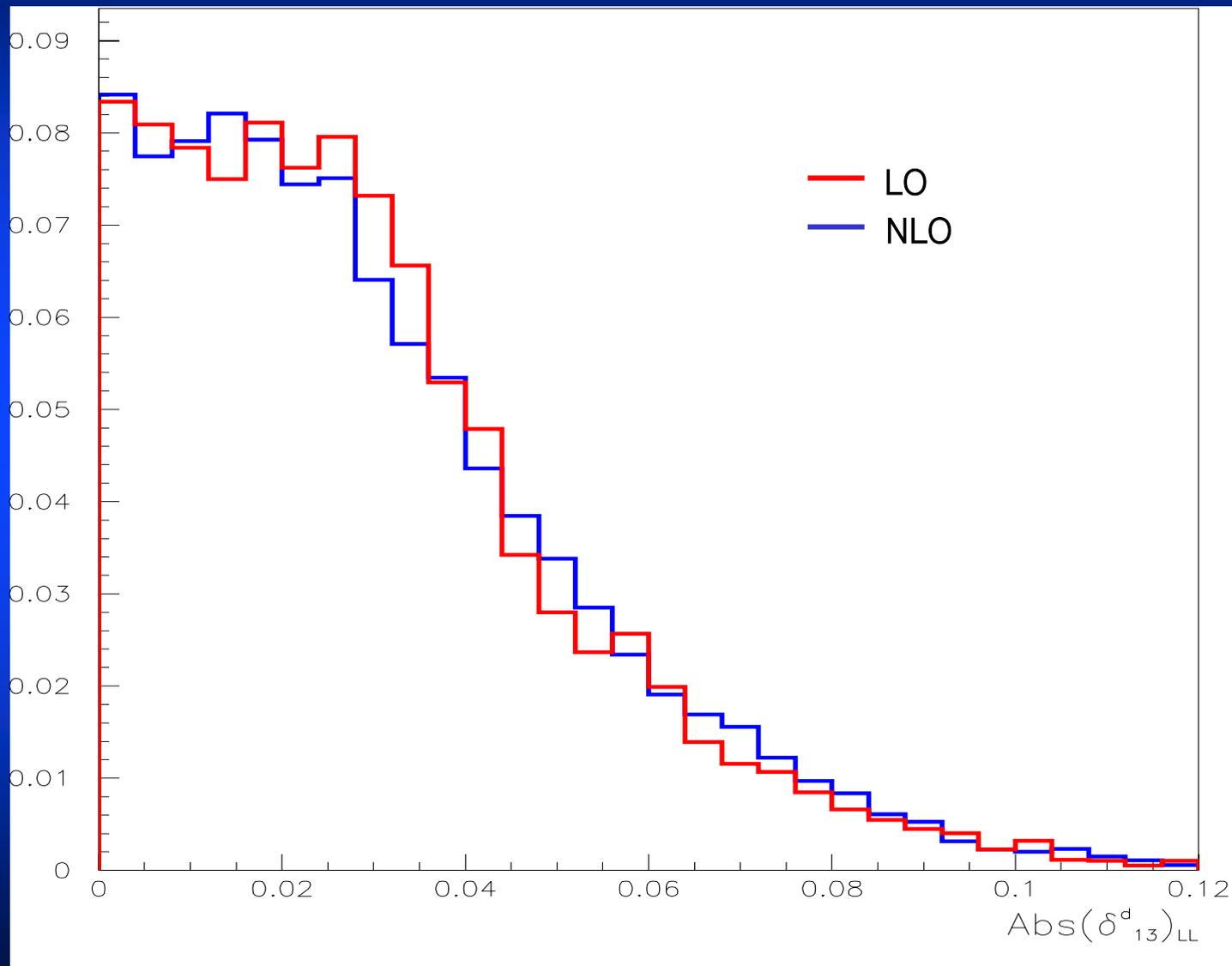
lower $m_{\tilde{g},\tilde{q}}$ and stringent δ 's

are both possible

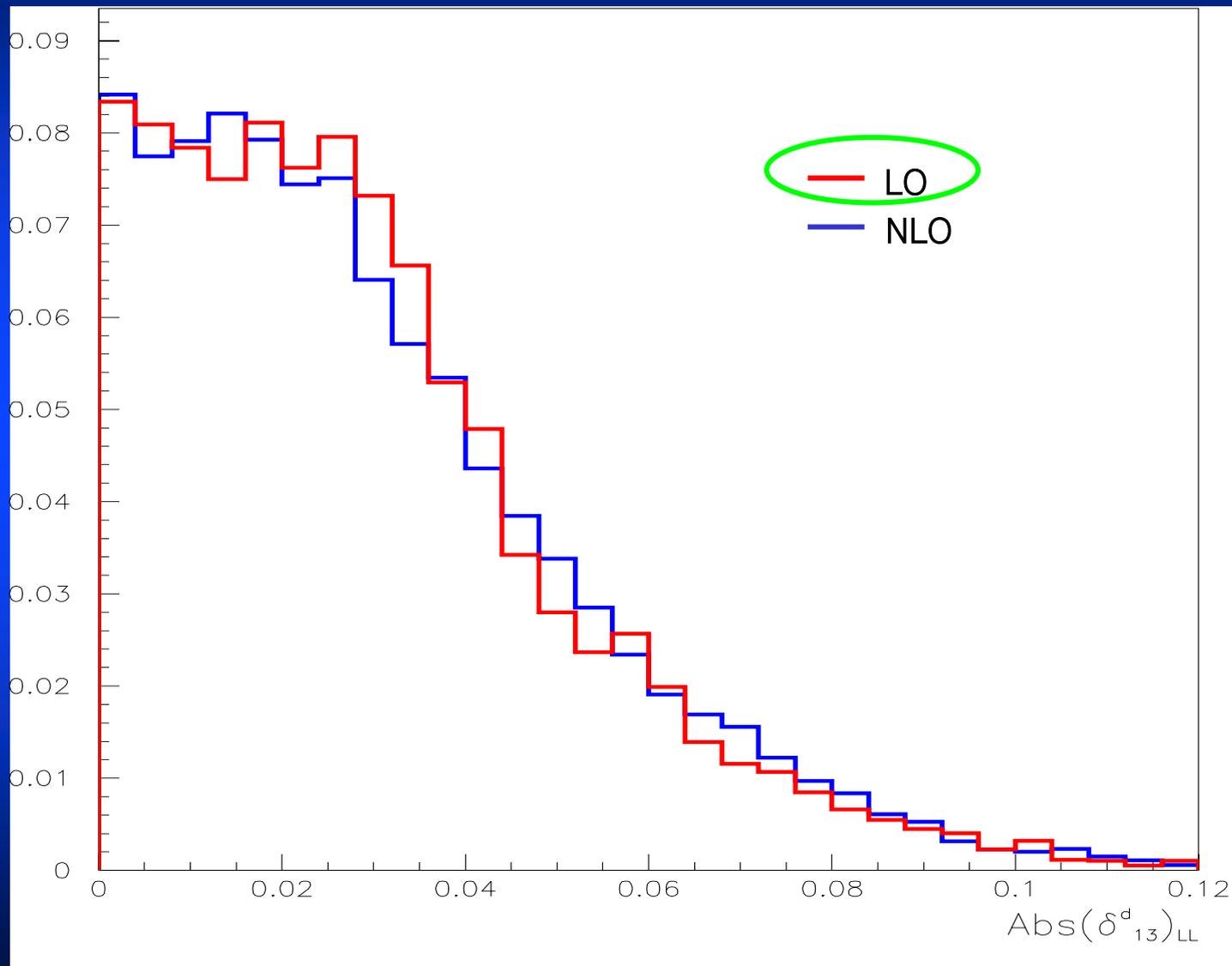
What is the effect of the NLO coefficients ?

- Depends on the mass insertion considered
- Doesn't alter the order of magnitude
- A direct comparison with previous analyses is not possible, but the improvements on the bounds appears mainly due to the higher precision of the recent measures.
- A major effect is due to the NLO evolution with respect to the LO evolution
- Weakens the dependence on the matching scale

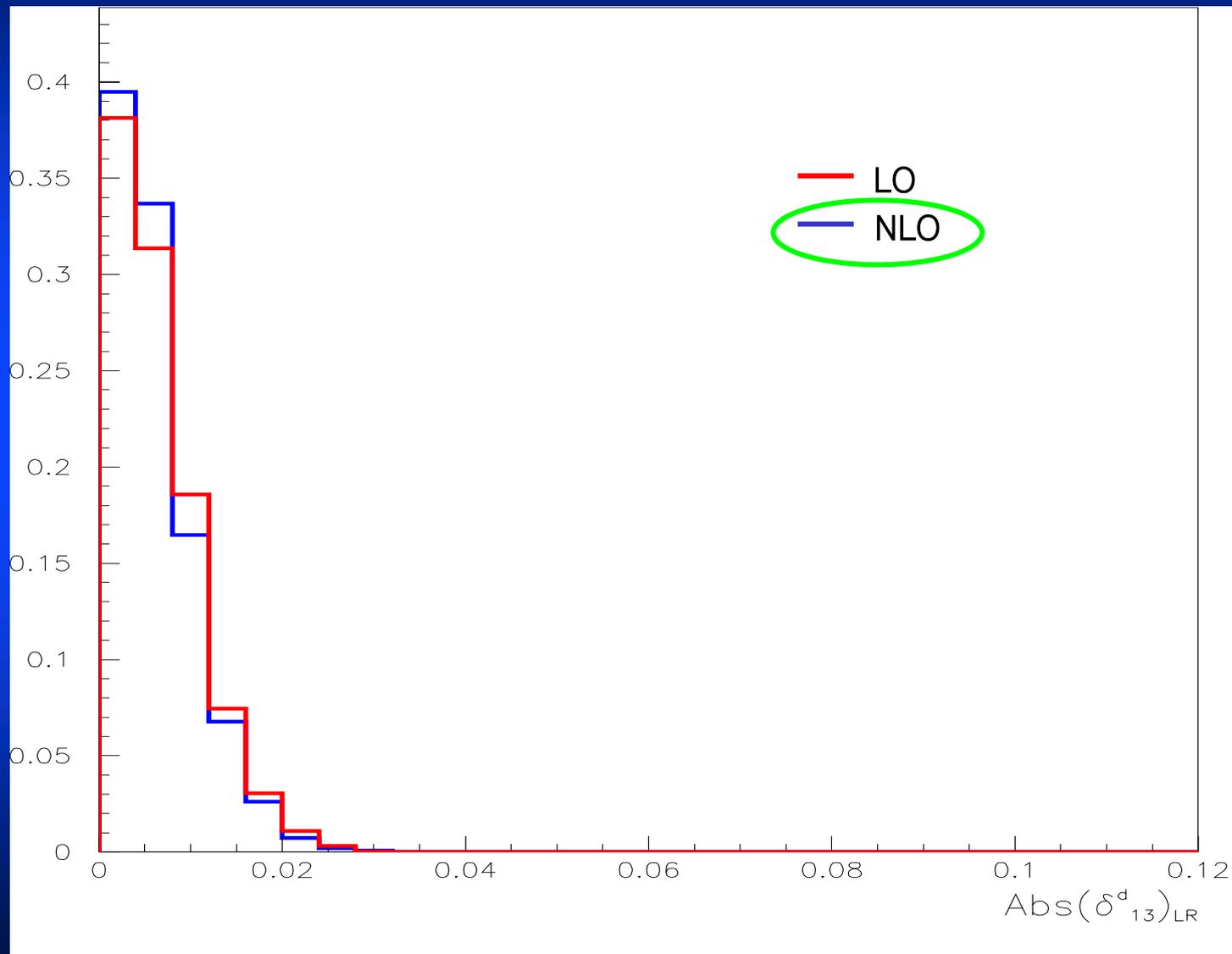
$$\left| (\delta_{13}^d)_{LL} \right|$$



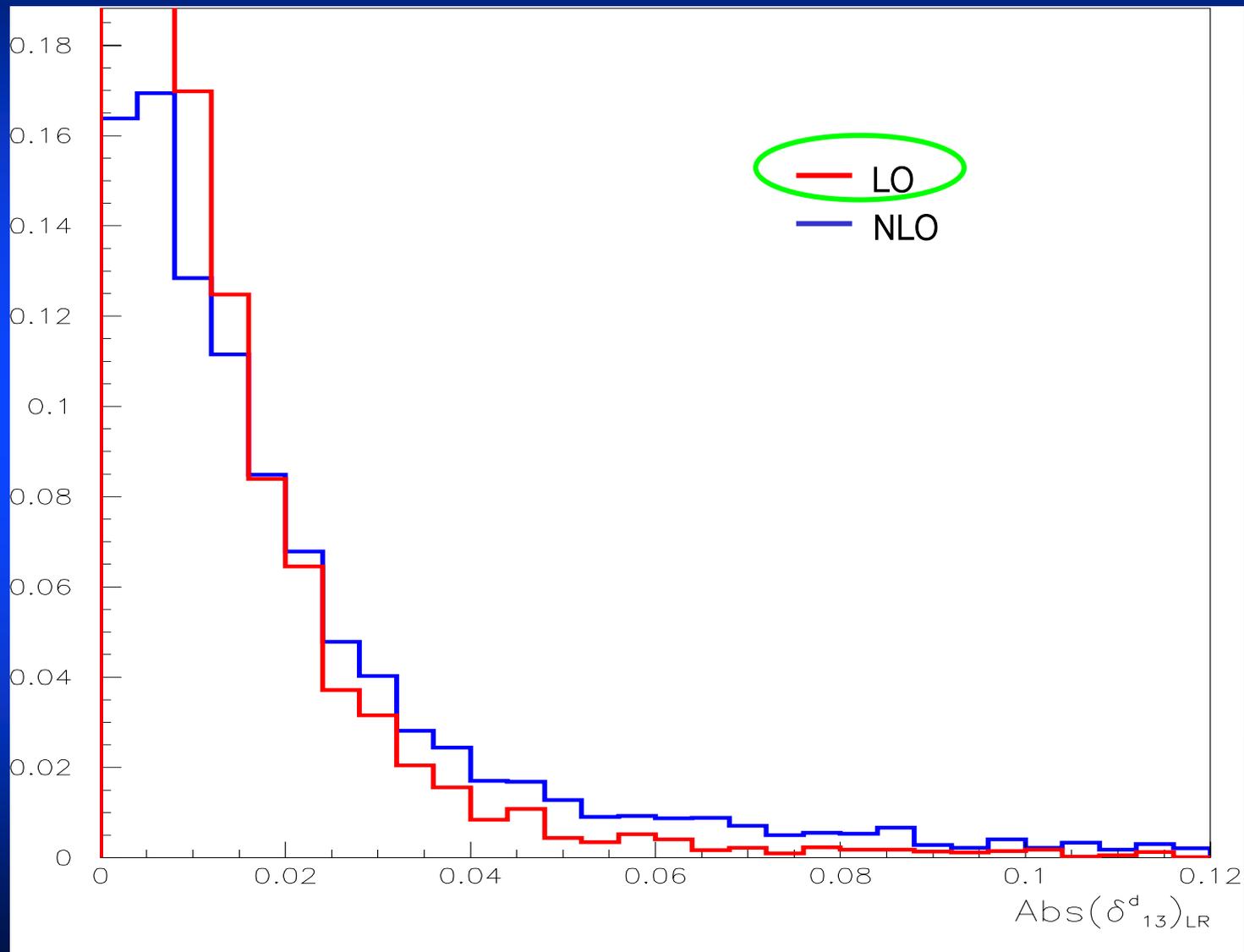
$$\left| (\delta_{13}^d)_{LL} \right|$$



$$\left| (\delta_{13}^d)_{LR} \right|$$

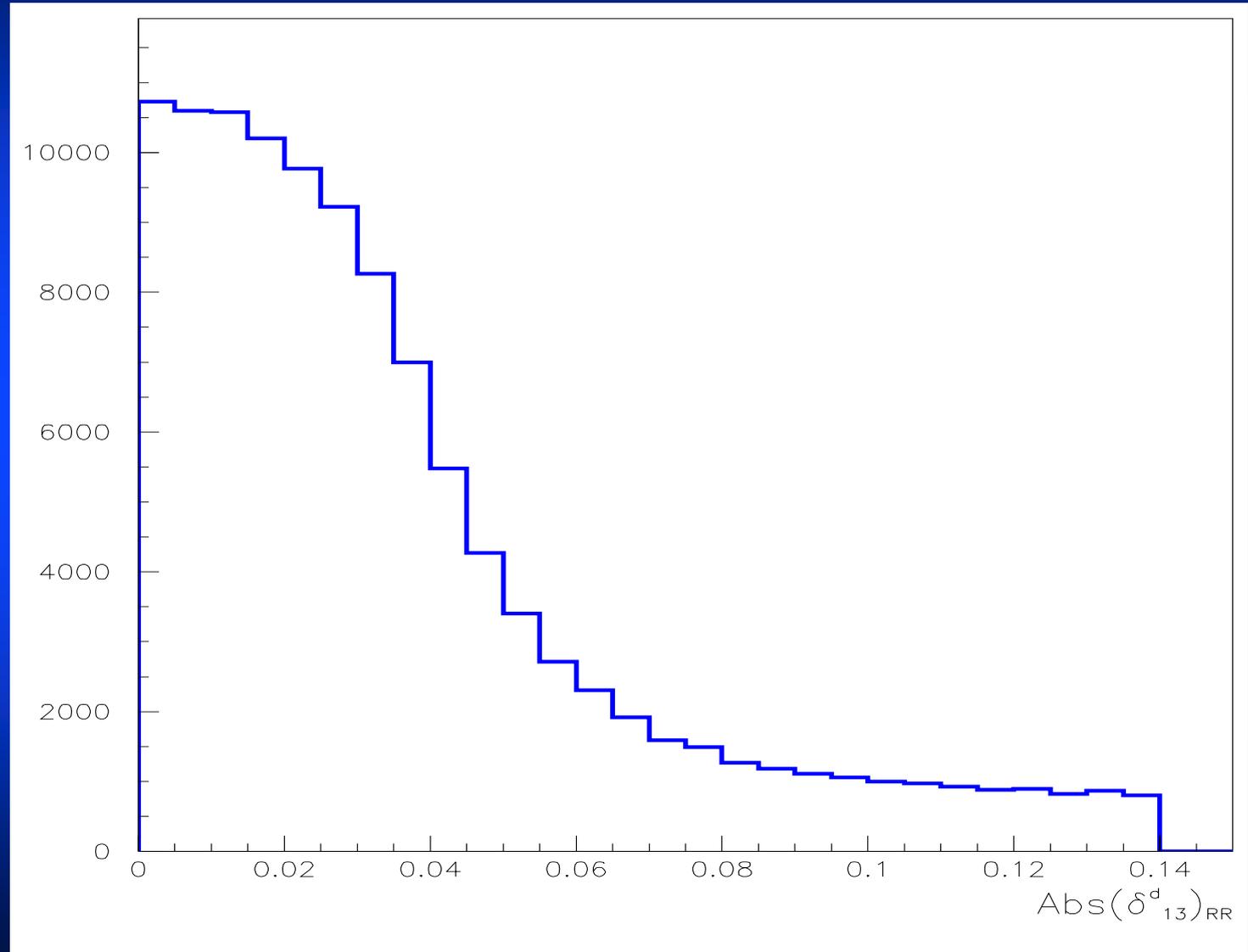


$$\left| (\delta_{13}^d)_{LR=RL} \right|$$

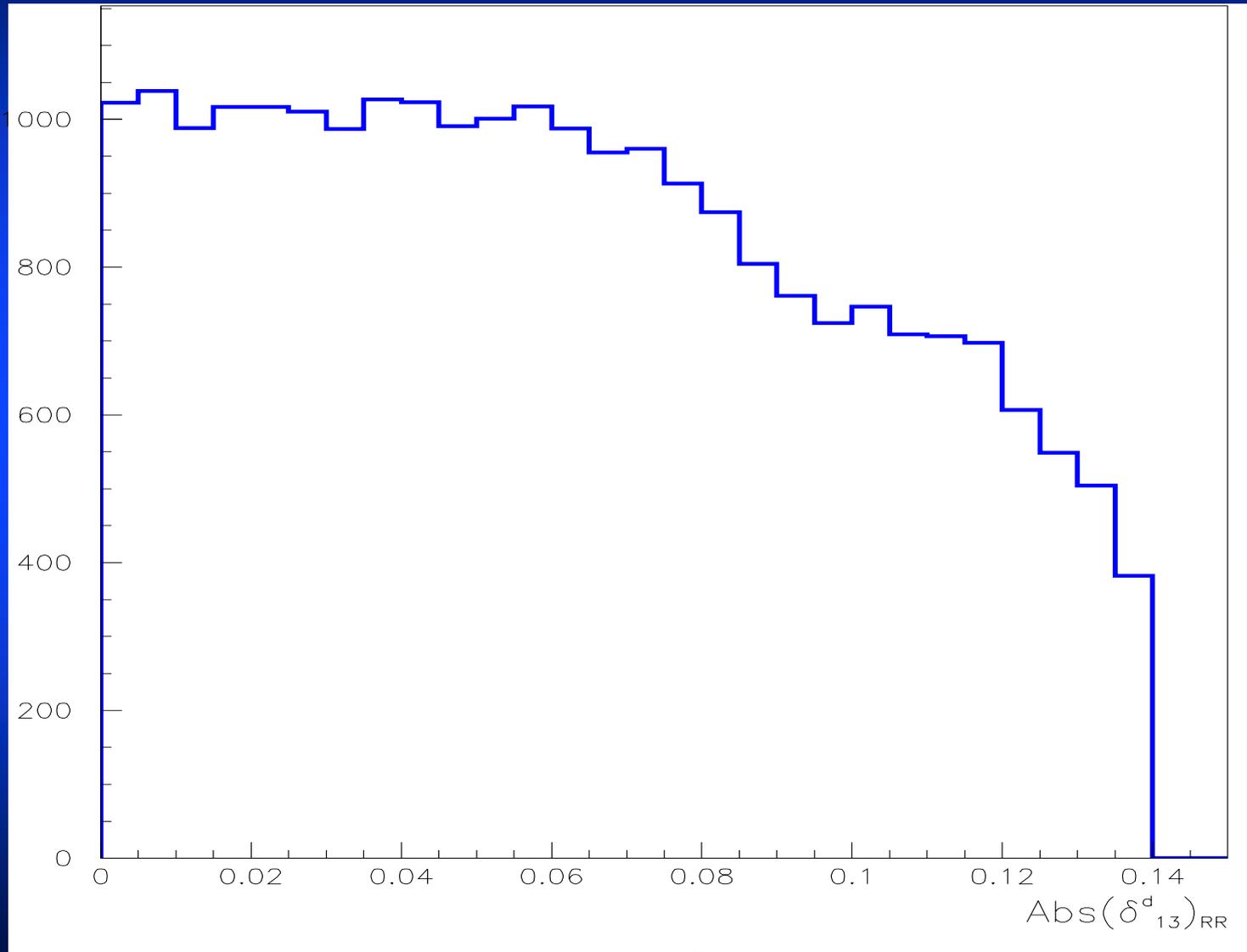


What is the effect of every experimental bound on the δ 's?

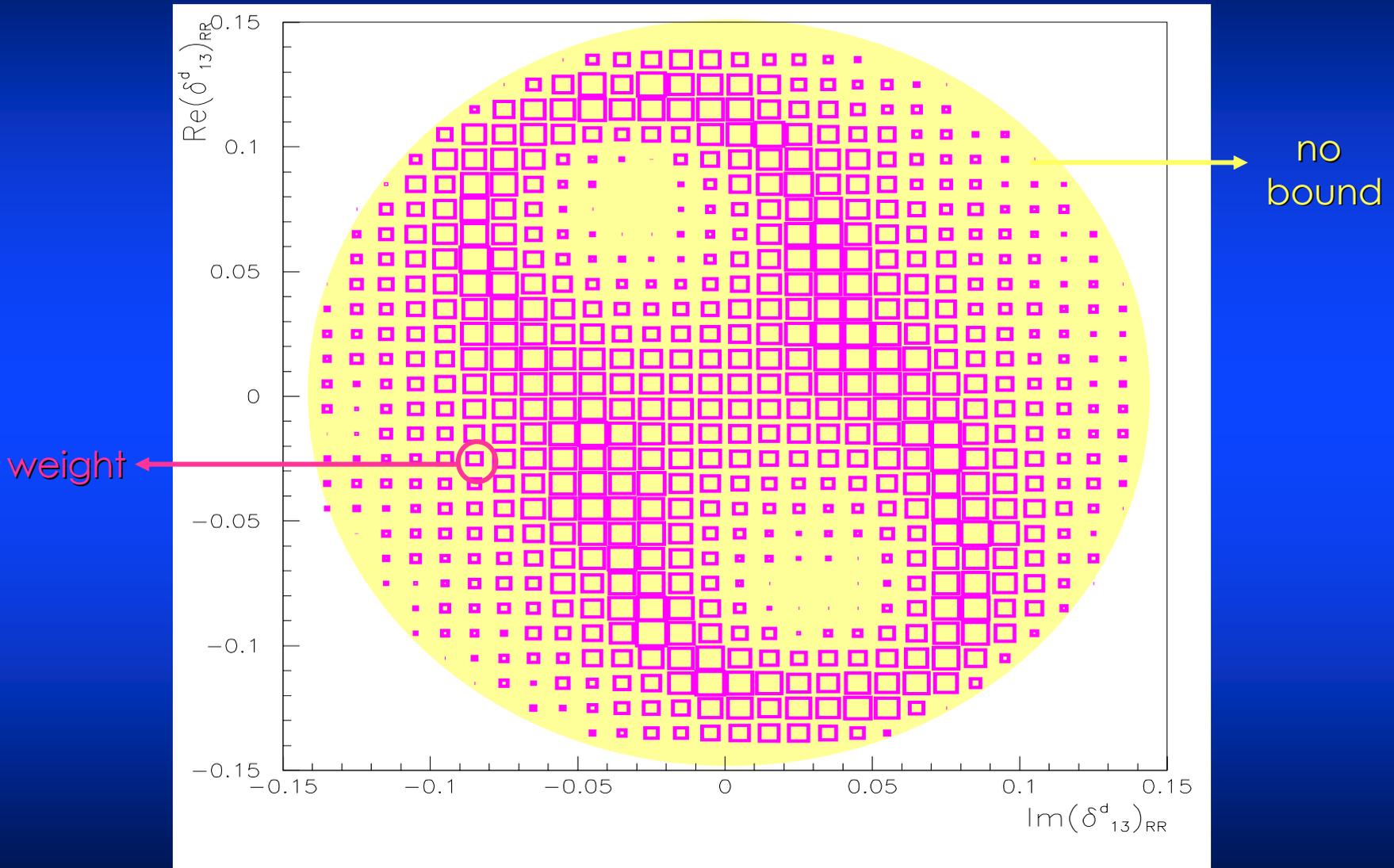
$\sin 2\beta$ on $|(\delta_{13}^d)_{RR}|$



Δm_d on $|\delta_{13}^d|_{RR}$

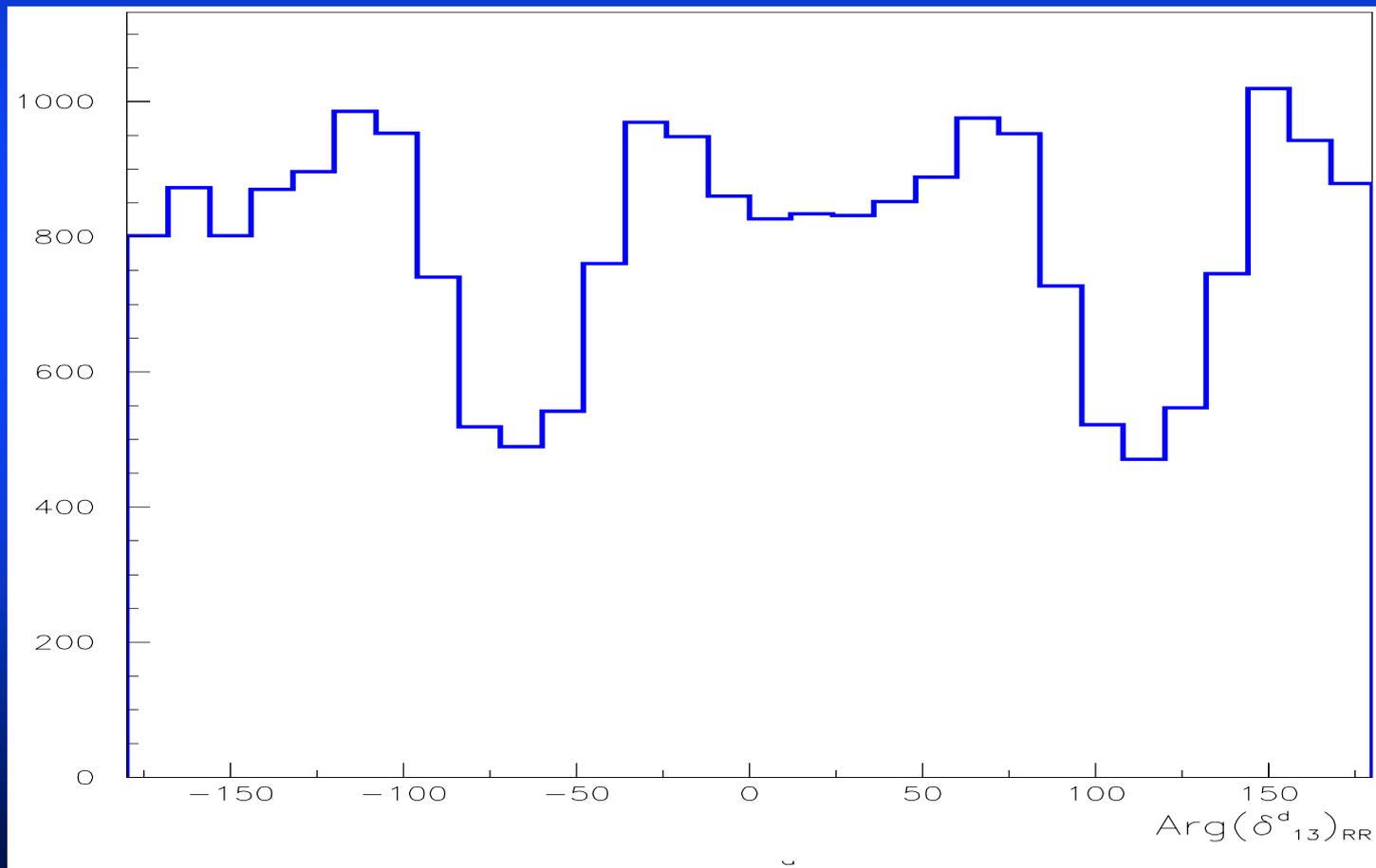


Δm_d



projected on $\text{Arg}(\delta_{13}^d)_{RR}$

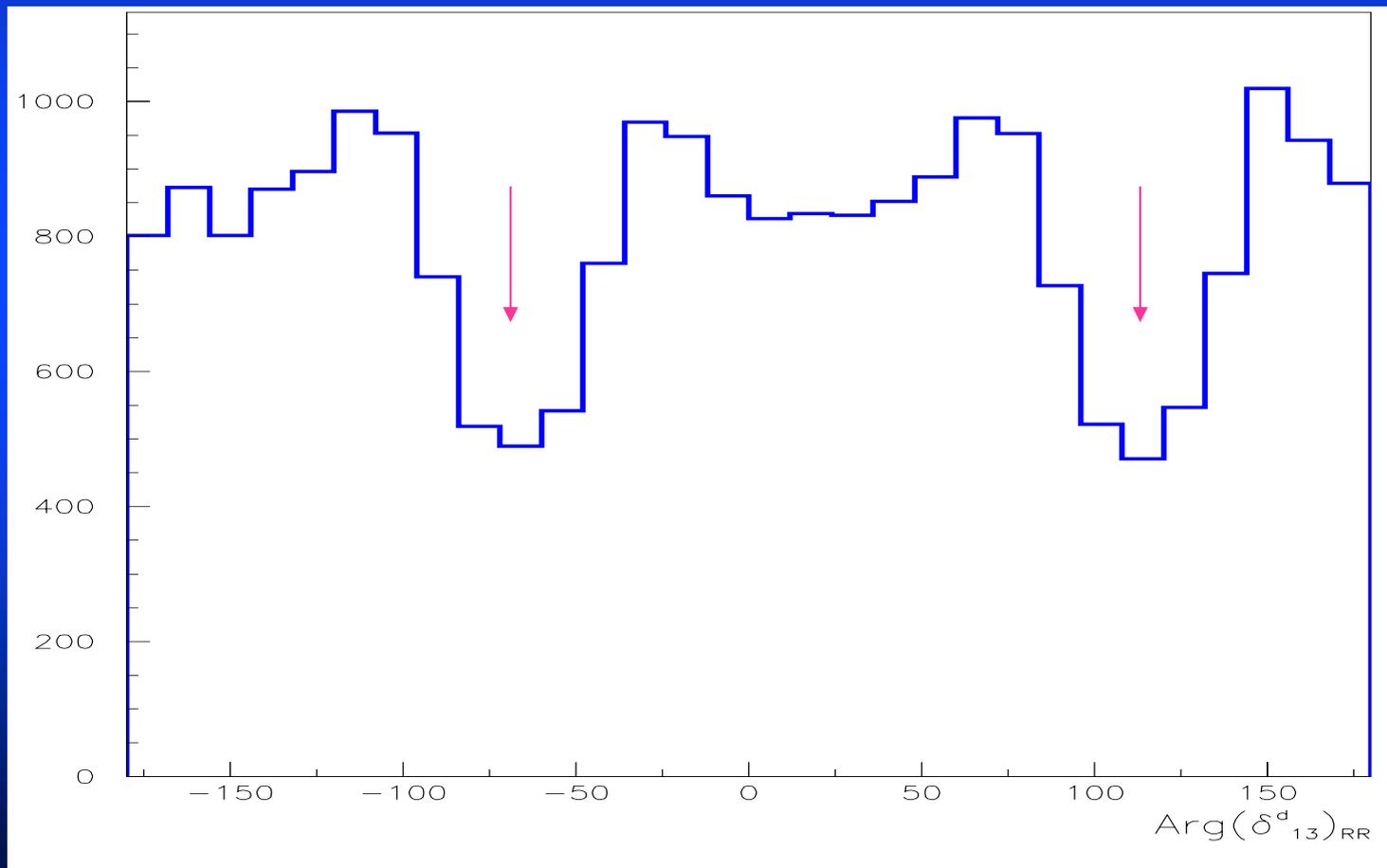
$$\Delta m_d = 2 |\langle \bar{B}_d | \mathcal{H}^{\Delta B=2} | B_d \rangle| = 2 |A_{SM} e^{i2\beta} + A_{SUSY} e^{i2\phi}|$$



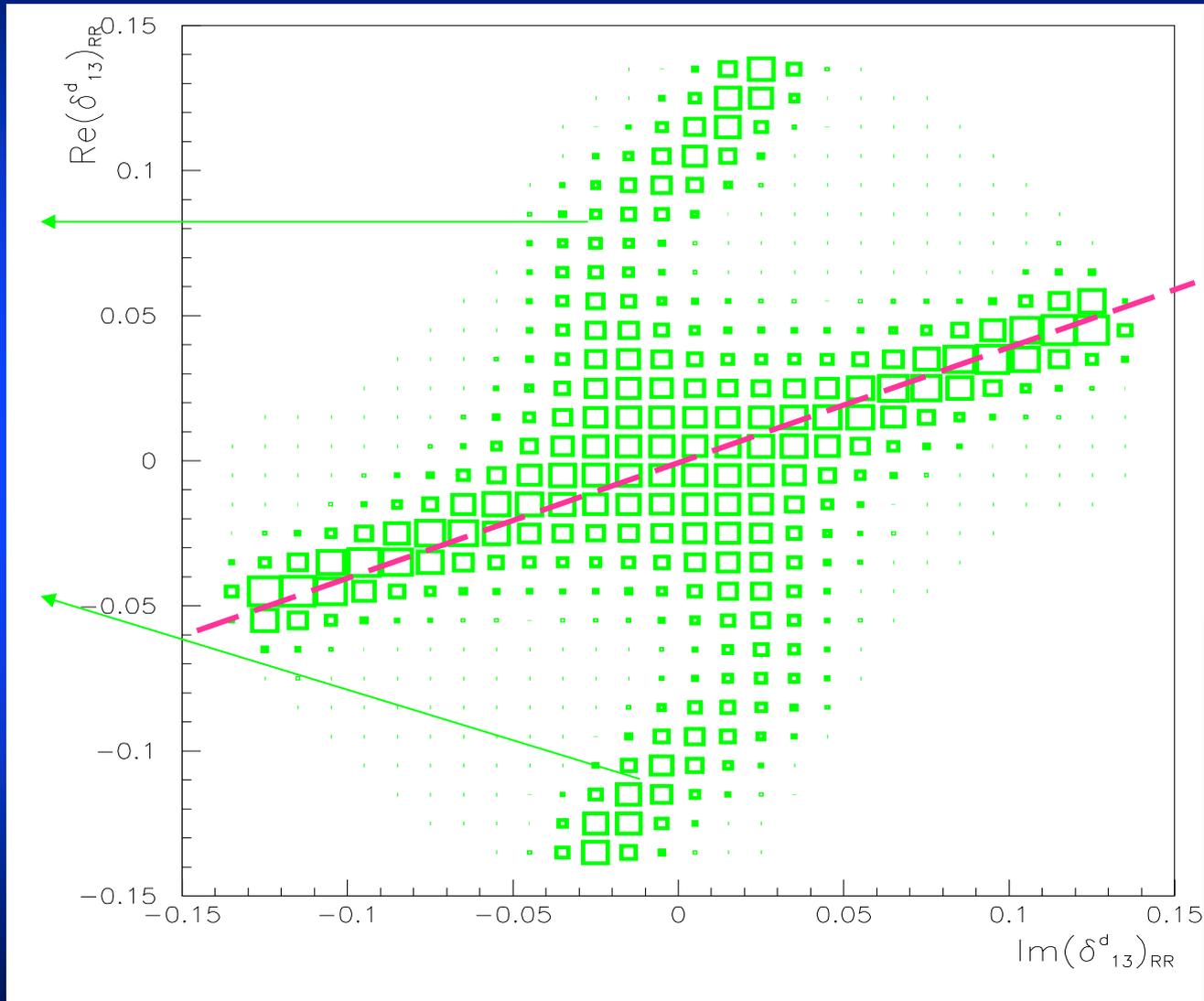
projected on $\text{Arg}(\delta_{13}^d)_{RR}$

$$\Delta m_d = 2 |\langle \bar{B}_d | \mathcal{H}^{\Delta B=2} | B_d \rangle| = 2 |A_{SM} e^{i2\beta} + A_{SUSY} e^{i2\phi}|$$

if $\phi = \pm \beta$ SUSY contribution is quadratic, otherwise linear



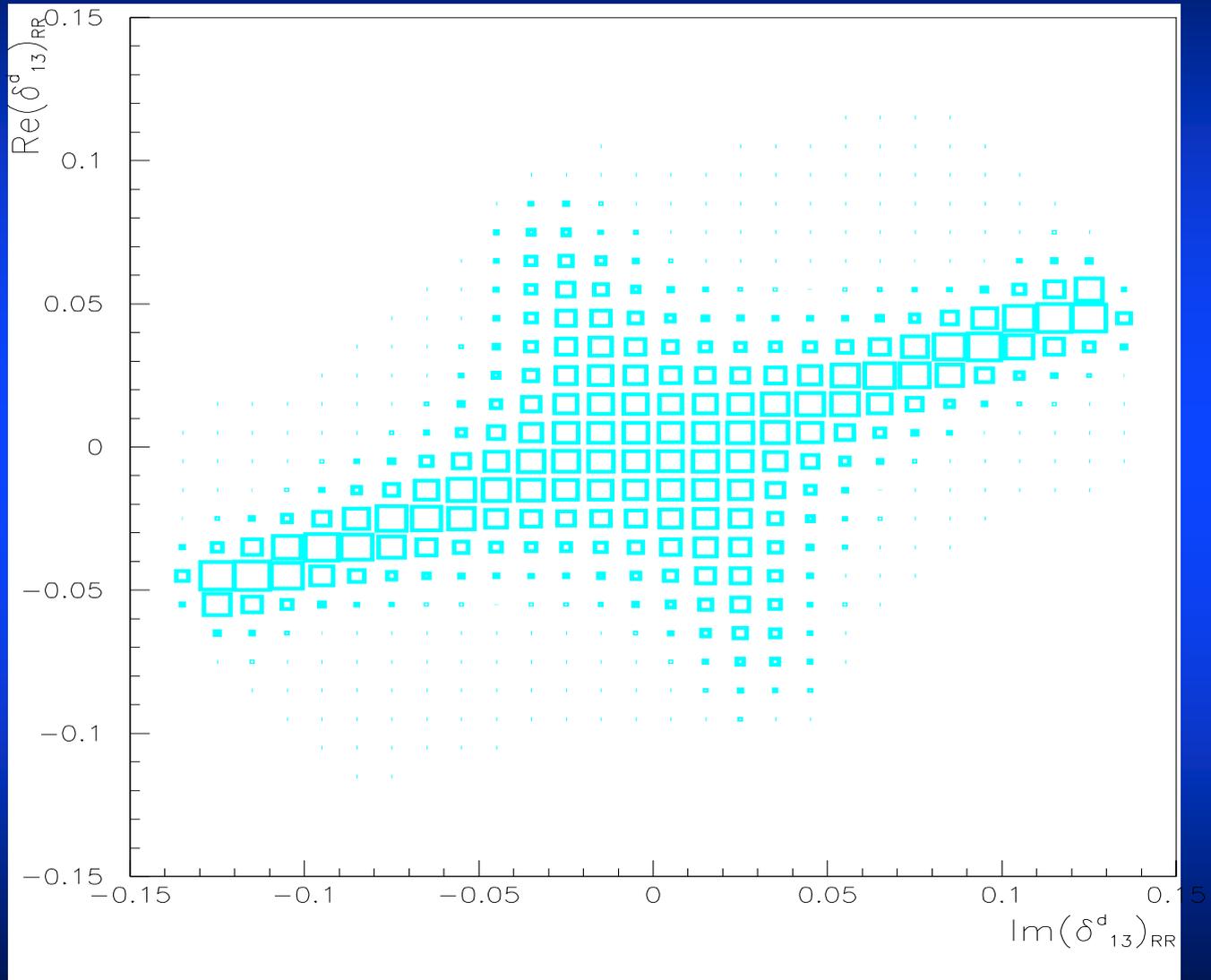
$\sin 2\beta$



Wrong
sign
branches

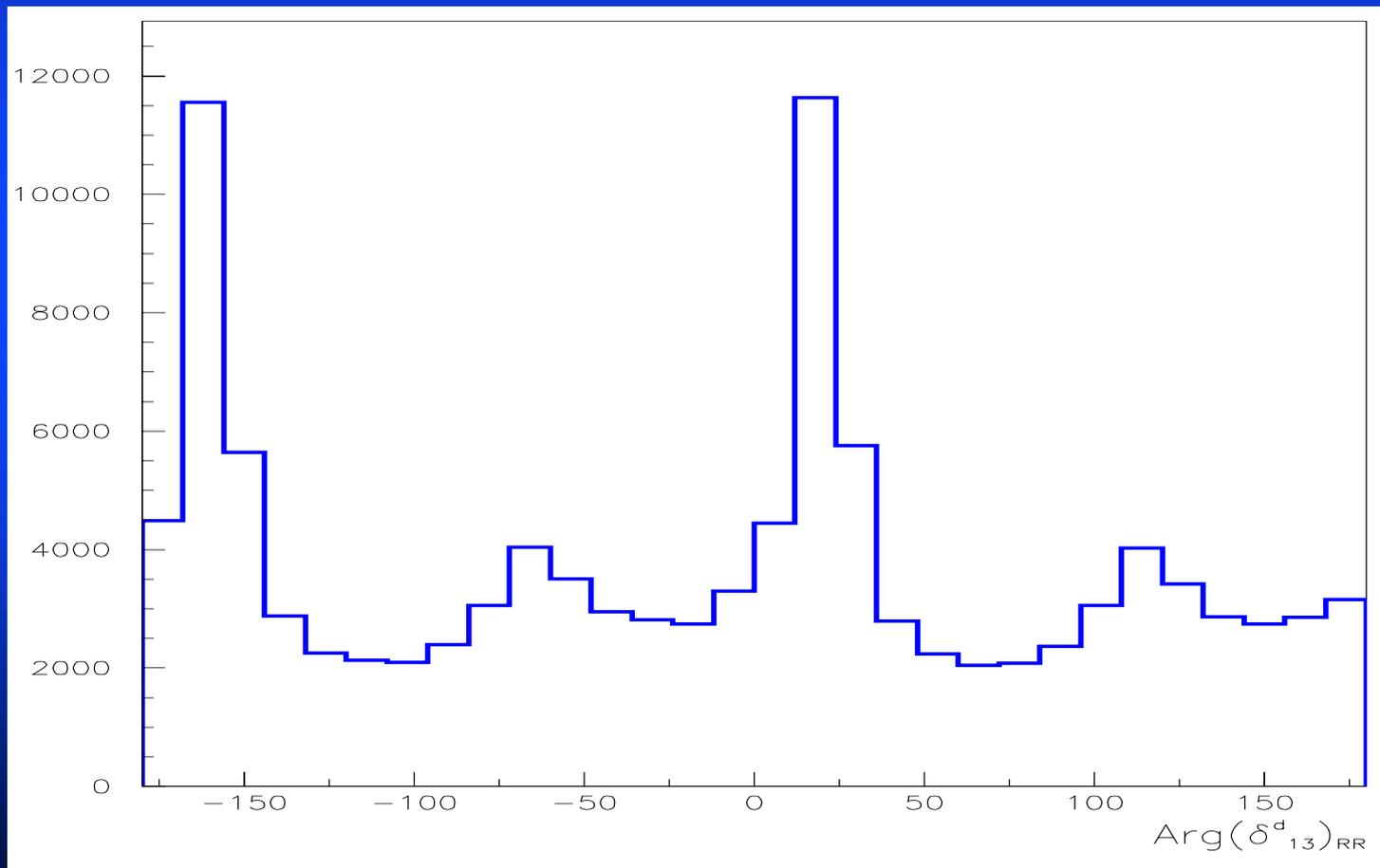
Note
the non
uniform
weights

$\sin 2\beta$ and $\cos 2\beta$



projected on $\text{Arg}(\delta_{13}^d)_{RR}$

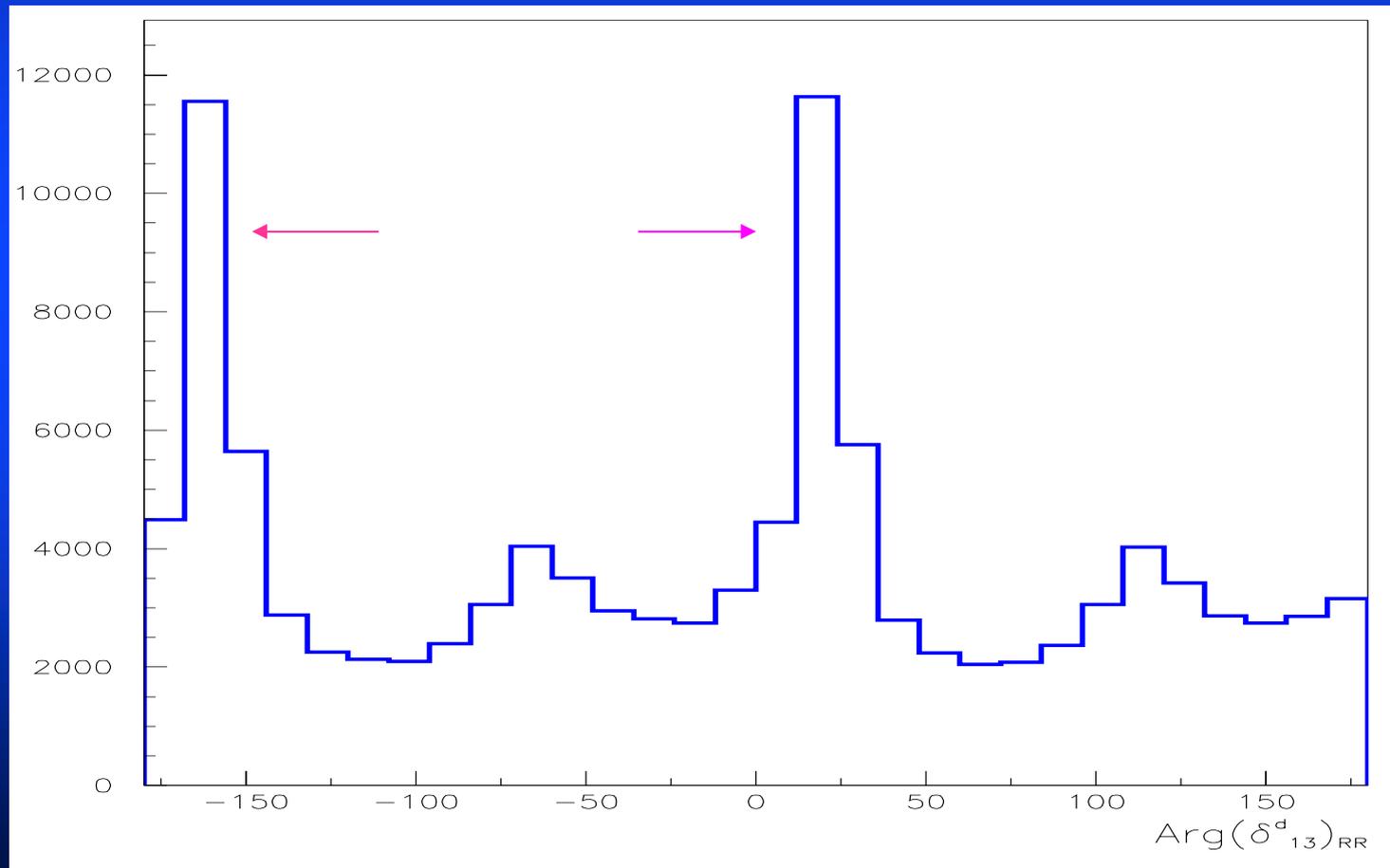
$$2\beta = \text{Arg} |\langle \bar{B}_d | \mathcal{H}^{\Delta B=2} | B_d \rangle| = \text{Arg} |A_{SM} e^{i2\beta} + A_{SUSY} e^{i2\phi}|$$



projected on $\text{Arg}(\delta_{13}^d)_{RR}$

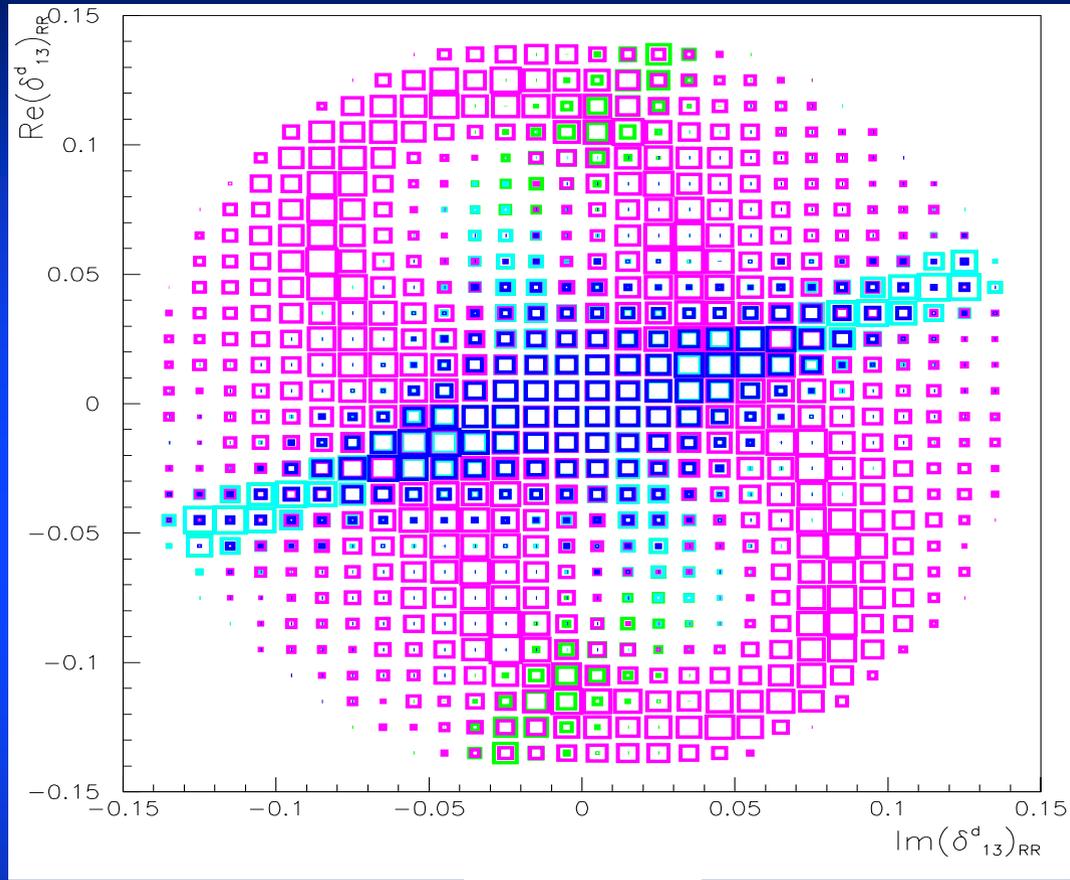
$$2\beta = \text{Arg} |\langle \bar{B}_d | \mathcal{H}^{\Delta B=2} | B_d \rangle| = \text{Arg} |A_{SM} e^{i2\beta} + A_{SUSY} e^{i2\phi}|$$

if $\phi = \beta$ the bound is satisfied for every A_{SUSY}

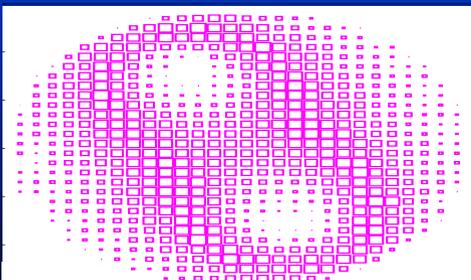


All the bounds
together:

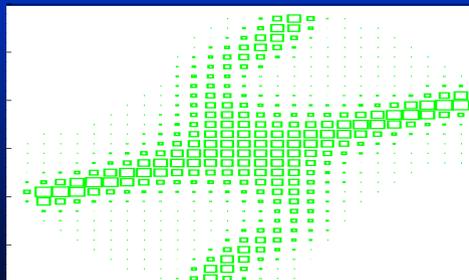
allowed region: dark blue squares



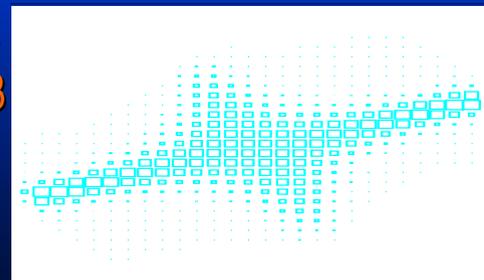
Δm_d



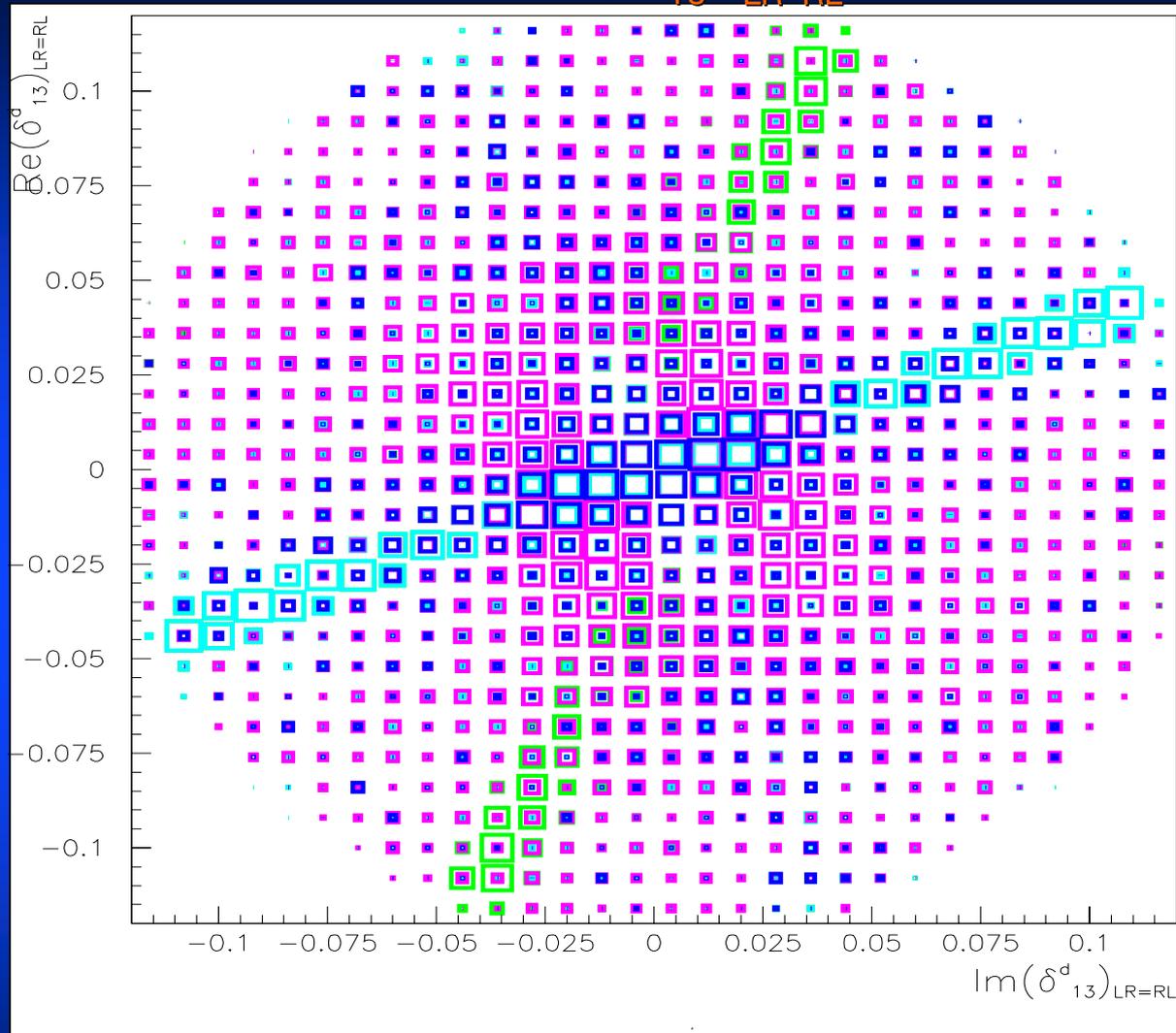
$\sin 2\beta$



$\cos 2\beta$

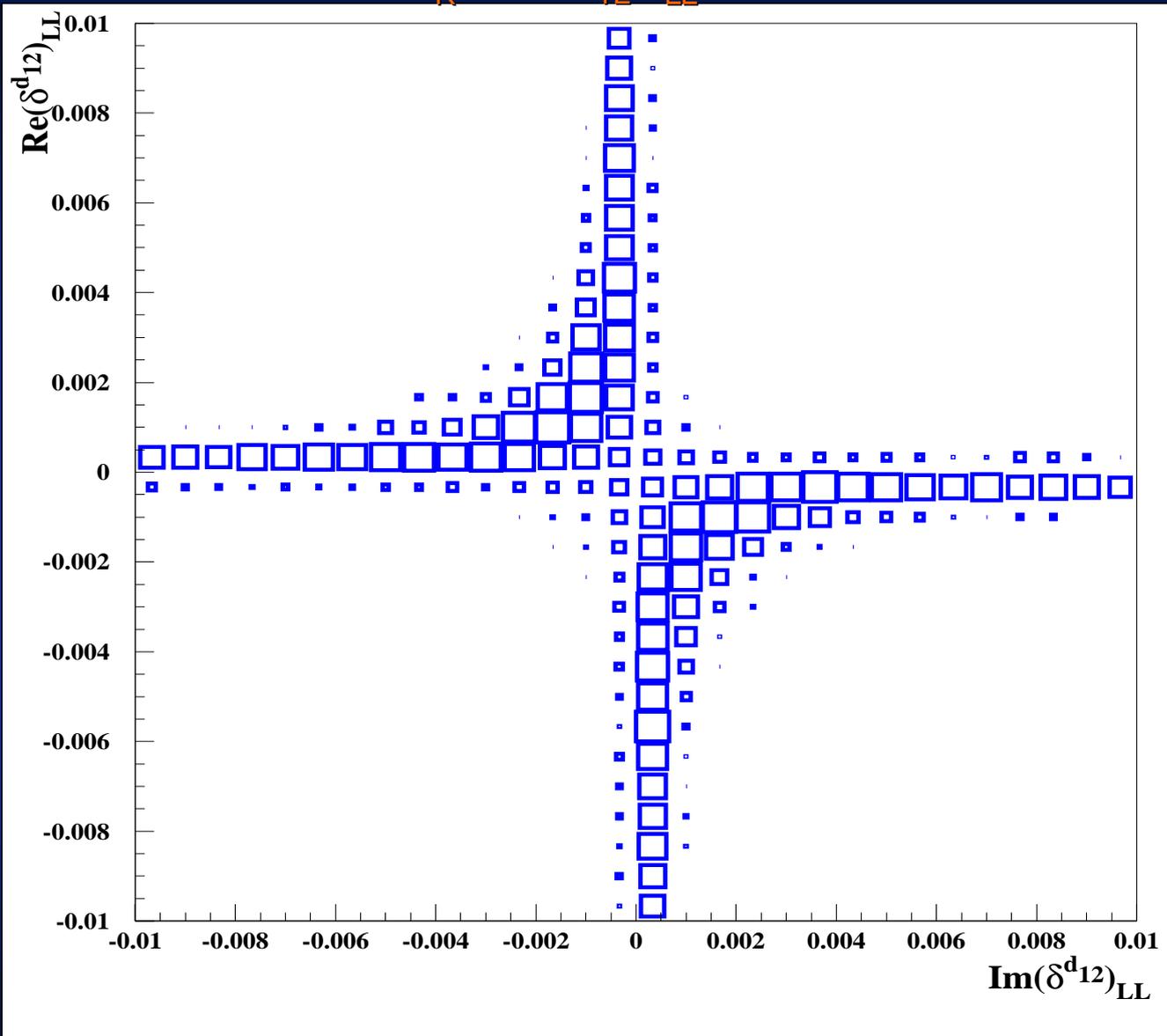


The same for $(\delta_{13}^d)_{LR=RL}$

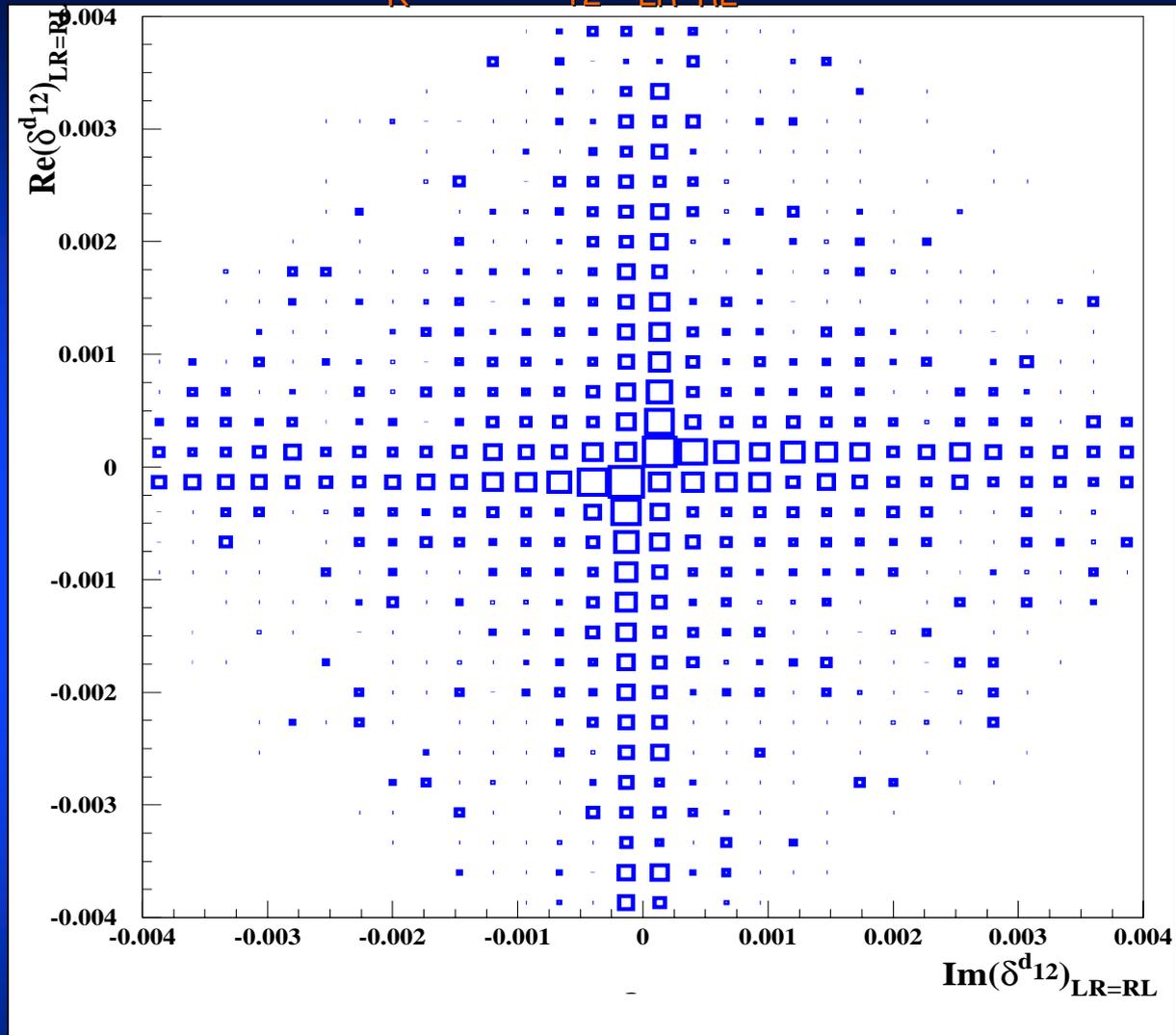


A partial cancellation in the Wilson coefficients occurs:
the bounds are less effective, the plot is more scattered

ϵ_K on $(\delta_{12}^d)_{LL}$



ε_K on $(\delta_{12}^d)_{LR=RL}$



Again an interference effect . Usually SUSY models with dominant LR/RL mass insertions can contribute more to ε'_K