

Playing with fermion couplings in Higgsless models

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- Introduction
- A $SU(2)_L \times SU(2)^K \times U(1)$ linear moose
- Electroweak precision tests
- Unitarity bounds
- Delocalizing fermion interactions
- Conclusions

Based on:

Casalbuoni, De Curtis, D., PRD hep-ph/0405188

Casalbuoni, De Curtis, Dolce, D., PRD hep-ph/05022209

(Modern) Higgsless Models

- ❖ **Symmetry breaking mechanism of a gauge theory in $4 + 1$ dims by boundary conditions on the branes.** (Csáki, Grojean, Murayama, Pilo, Terning; Nomura).
- ❖ **The scale where partial wave unitarity is lost is delayed with respect to the SM without the Higgs, due the exchange of KK excitations of gauge bosons.** (Chivukula, Dicus, He).
- ❖ **Problem: $\epsilon_3(S)$ electroweak parameter too big, if unitarity is fine** (Barbieri, Pomarol, Rattazzi).
- ❖ **Solutions:**
 - brane kinetic terms** (Cacciapaglia, Csaki, Grojean, Terning; Carena, Tait, Wagner; Carena, Ponton Tait, Wagner; Davoudiasl, Hewett, Lillie, Rizzo).
 - fermion delocalization** (Cacciapaglia, Csaki, Grojean, Terning; Foadi, Gopalakrishna, Schmidt; Bhattacharya, Csaki, Martin, Shirman, Terning).

Alternative approach: dimensional deconstruction and moose models
(Arkani-Hamed, Cohen, Georgi)

Theory with gauge symmetry $[G]^{K+1}$ in $3 + 1$ dims:

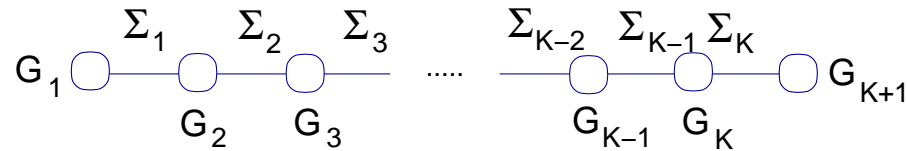
$$A^j = A^{ja} T^a, \quad g_c; \quad j = 1, \dots, K + 1.$$

Non linear σ -model fields:

$$\Sigma_i = e^{i/(2f_c)\pi^a T^a}, \quad \Sigma_i \rightarrow U_i \Sigma_i U_{i+1}^\dagger, \quad U_i \in G_i, \quad i = 1, 2, \dots, K.$$

Covariant derivatives: $D_\mu \Sigma_i = \partial_\mu \Sigma_i - ig_c A_\mu^i \Sigma_i + ig_c \Sigma_i A_\mu^{i+1}$.

$$\mathcal{L}_{moose} = \sum_{i=1}^K f_c^2 \text{Tr}[D_\mu \Sigma_i^\dagger D^\mu \Sigma_i] - \frac{1}{2} \sum_{i=1}^{K+1} \text{Tr}[(F_{\mu\nu}^i)^2].$$



Mass spectrum

Mass matrix $\{A_\mu^1, A_\mu^2, \dots, A_\mu^{K+1}\}$:

$$M^2 = g_c^2 f_c^2 \begin{pmatrix} 1 & -1 & 0 & \dots & 0 & 0 \\ -1 & 2 & -1 & \dots & 0 & 0 \\ 0 & -1 & 2 & \ddots & 0 & 0 \\ \vdots & \vdots & \ddots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & 2 & -1 \\ 0 & 0 & 0 & \dots & -1 & 1 \end{pmatrix}.$$

Mass eigenvalues:

$$M_k^2 = 4g_c^2 f_c^2 \sin^2 \left(\frac{\pi k}{2(K+1)} \right) \longrightarrow \left(\frac{k}{R} \right)^2 : \quad |k| \ll K.$$

For $|k| \ll K$ they reproduce the masses of KK excitations for a five dimensional theory with gauge symmetry G , compactification radius R , gauge coupling g_5 , lattice spacing a ,

$$\pi R = (K+1)a, \quad \frac{a}{g_5^2} = \frac{1}{g_c^2} : \quad a = \frac{1}{g_c f_c}.$$

Extra dimension on a lattice

(Hill, Pokorski, Wang; Randall, Shadmi, Weiner; Abe, Kobayashi, Maru, Yoshioka)

Theory with gauge symmetry G in $4 + 1$ dims and flat metric:

$$\begin{aligned}
 S &= -\frac{1}{2} \int d^4x \int_0^{\pi R} dy \frac{1}{g_5^2} [\text{Tr}[F_{MN}F^{MN}]], \quad M, N = 0, 1, \dots, 4 \\
 &= -\frac{1}{2} \int d^4x \int_0^{\pi R} dy \frac{1}{g_5^2} [\text{Tr}[F_{\mu\nu}F^{\mu\nu}] + 2\text{Tr}[F_{\mu 5}F^{\mu 5}]]
 \end{aligned}$$

↓ discretization of extra dim on a lattice

$$S_{moose} \sim -\frac{1}{2} \int d^4x \frac{a}{g_5^2} \sum_j \left[\text{Tr}[F_{\mu\nu}^j F^{\mu\nu j}] + \frac{2}{a^2} \text{Tr}[(D_\mu \Sigma^j)^\dagger (D^\mu \Sigma^j)] \right],$$

where

$$\Sigma^j \sim e^{i \int_{y_j}^{y_j+a} dt A_5(x,t)} \Rightarrow D_\mu \Sigma^j \sim a F_{\mu 5}^j = ia \partial_\mu A_5^j - i(A_\mu^{j+1} - A_\mu^j).$$

Gauge theories with replicas of $G \Leftrightarrow$ compactified dimensions.

A $SU(2)_L \times SU(2)^K \times U(1)$ linear moose

(Casalbuoni, De Curtis, D., see also Foadi, Gopalakrishna, Schmidt; Hirn, Stern; Chivukula et al; Georgi)



The transformation properties of the fields are

$$\Sigma_1 \rightarrow L \Sigma_1 U_1^\dagger,$$

$$\Sigma_i \rightarrow U_{i-1} \Sigma_i U_i^\dagger, \quad i = 2, \dots, K,$$

$$\Sigma_{K+1} \rightarrow U_K \Sigma_{K+1} R^\dagger,$$

$$U_i \in G_i \equiv SU(2)_i, \quad i = 1, 2, \dots, K \quad A_\mu^i = A_\mu^{ia} \tau^a / 2, \quad g_i,$$

$$L \in G_L \equiv SU(2)_L \quad \tilde{W}_\mu = \tilde{W}_\mu^a \tau^a / 2, \quad \tilde{g},$$

$$R \in G_R \equiv SU(2)_R \supset U(1)_Y \quad \tilde{Y}_\mu = \tilde{Y}_\mu \tau^3 / 2, \quad \tilde{g}'.$$

$$\mathcal{L} = \sum_{i=1}^{K+1} f_i^2 \text{Tr}[D_\mu \Sigma_i^\dagger D^\mu \Sigma_i] - \frac{1}{2} \sum_{i=1}^K \text{Tr}[(F_{\mu\nu}^i)^2] - \frac{1}{2} \text{Tr}[(F_{\mu\nu}(\tilde{W}))^2] - \frac{1}{2} \text{Tr}[(F_{\mu\nu}(\tilde{Y}))^2].$$

Covariant derivatives

$$D_\mu \Sigma_1 = \partial_\mu \Sigma_1 - i\tilde{g}\tilde{W}_\mu \Sigma_1 + i\Sigma_1 g_1 A_\mu^1,$$

$$D_\mu \Sigma_i = \partial_\mu \Sigma_i - i g_{i-1} A_\mu^{i-1} \Sigma_i + i \Sigma_i g_i A_\mu^i, \quad i = 2, \dots, K,$$

$$D_\mu \Sigma_{K+1} = \partial_\mu \Sigma_{K+1} - i g_K A_\mu^K \Sigma_{K+1} + i\tilde{g}' \Sigma_{K+1} \tilde{Y}_\mu.$$

Global symmetry: $SU(2)_L \times SU(2)^K \times SU(2)_R$.

We assume **standard fermionic couplings w.r.t.** $SU(2)_L \otimes U(1)_Y$.

Therefore fermions are located at the end of the moose (ψ_L (ψ_R) to the left (right) end).

$f_i = f_c \forall i \Rightarrow$ flat metric in five dims; varying $f_i \Rightarrow$ warped metric.

At the leading order in $O((\tilde{g}/g_i)^2)$

$$\tilde{M}_W^2 = \frac{v^2}{4} \tilde{g}^2, \quad \tilde{M}_Z^2 = \tilde{M}_W^2 / \tilde{c}_\theta^2, \quad \tan \tilde{\theta} = \frac{\tilde{g}}{\tilde{g}'};$$

$$\frac{4}{v^2} \equiv \frac{1}{f^2} = \sum_{i=1}^{K+1} \frac{1}{f_i^2}$$

Electroweak precision tests

The mass matrix of the A_i gauge fields:

$$\mathcal{L}_{\text{mass}} = \frac{1}{2} \sum_{i,j=1}^K (M_2)_{ij} A_\mu^i A^{\mu j},$$

with

$$(M_2)_{ij} = g_i^2 (f_i^2 + f_{i+1}^2) \delta_{i,j} - g_i g_{i+1} f_{i+1}^2 \delta_{i,j-1} - g_j g_{j+1} f_{j+1}^2 \delta_{i,j+1}.$$

Calling \tilde{A}_μ^n , $n = 1, \dots, K$ the mass eigenstates, and m_n^2 the squared mass eigenvalues,

$$A_\mu^i = \sum_{n=1}^K S_n^i \tilde{A}_\mu^n,$$

$$S_m^i (M_2)_{ij} S_n^j = m_n^2 \delta_{m,n}.$$

Custodial symmetry: $\epsilon_1 = \epsilon_2 = 0$. **Dispersive representation:**

$$\epsilon_3 \left(= \frac{\tilde{g}^2 S}{16\pi} \right) = -\frac{\tilde{g}^2}{4\pi} \int_0^\infty \frac{ds}{s^2} \text{Im}[\Pi_{VV}(s) - \Pi_{AA}(s)]$$

Current current correlator:

$$\int d^4x e^{-iq \cdot x} \langle J_{V(A)}^\mu J_{V(A)}^\nu \rangle \sim i g^{\mu\nu} \Pi_{VV(AA)}(q^2) + \dots$$

The vector meson decay constants

$$\langle 0 | J_{V\mu}^a | \tilde{A}_b^n(p, \epsilon) \rangle = g_{nV} \delta^{ab} \epsilon_\mu,$$

$$\langle 0 | J_{A\mu}^a | \tilde{A}_b^n(p, \epsilon) \rangle = g_{nA} \delta^{ab} \epsilon_\mu,$$

$$\begin{aligned} J_{V(A)\mu}^a \Big|_{\text{vector mesons}} &= f_1^2 g_1 A_\mu^{1a} + (-) f_{K+1}^2 g_K A_\mu^{Ka}, \\ g_{nV(A)} &= f_1^2 g_1 S_n^1 + (-) f_{K+1}^2 g_K S_n^K \end{aligned}$$

Vector meson dominance

$$\epsilon_3 = \frac{\tilde{g}^2}{4} \sum_n \left(\frac{g_{nV}^2}{m_n^4} - \frac{g_{nA}^2}{m_n^4} \right) = \tilde{g}^2 g_1 g_K f_1^2 f_{K+1}^2 (M_2^{-2})_{1K} = \tilde{g}^2 \sum_{i=1}^K \frac{(1 - y_i) y_i}{g_i^2}$$

where

$$y_i = \sum_{j=1}^i \frac{f_j^2}{f_j^2}$$

Since $0 \leq y_i \leq 1 \Rightarrow \epsilon_3 > 0$.

For $f_i = f_c, g_i = g_c$

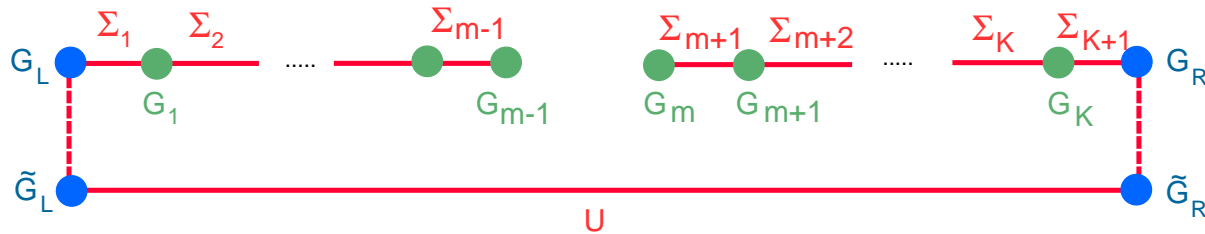
$$\epsilon_3 = \frac{1}{6} \frac{K(K+2)}{K+1} \frac{\tilde{g}^2}{g_c^2}$$

$\epsilon_3 \sim 10^{-3}$. For $K = 1 \Rightarrow g_c \sim 16\tilde{g}$. For increasing K , $g_c \sim 10\sqrt{K}$.

Possible solutions: Cutting a link

Let us suppose $\exists m : f_m = 0$, then the squared mass matrix becomes block diagonal, $\Rightarrow (M_2^{-2})_{1K} = 0 \Rightarrow \epsilon_3 = 0$ However we loose a link (and the corresponding scalar multiplet). We can add the term

$$f_0^2 \text{Tr}[\partial_\mu U^\dagger \partial^\mu U], \quad U = \Sigma_1 \Sigma_2 \cdots \Sigma_{K+1}$$



Dashed lines \Rightarrow the identification of the global symmetry groups after weak gauging. For $K = 2$ this model coincides with D-BESS (Casalbuoni et al)

Possible solutions: Suppressing a link

$$f_i = \bar{f} e^{c(i-1)}, \quad g_i = g_c \quad \epsilon_3 \sim \left(\frac{\tilde{g}}{g_c} \right)^2 e^{-2c}.$$

Partial wave unitarity bounds

(see also Chivukula, He; D., De Curtis, Pelaez; Papucci; Muck, Nilse, Pilaftsis, Ruckl)

Equivalence theorem, $\Sigma_i = \exp(i f \vec{\pi} \cdot \vec{\tau} / 2 f_i^2)$:

$$\begin{aligned} \mathcal{A}_{W_L^+ W_L^- \rightarrow W_L^+ W_L^-} &\sim \mathcal{A}_{\pi^+ \pi^- \rightarrow \pi^+ \pi^-} \\ &\sim -\frac{1}{4} f^4 \sum_{i=1}^{K+1} \frac{u}{f_i^6} + \frac{1}{4} f^4 \sum_{i=1}^{K+1} L_{ij} \left(\frac{u-t}{(s-M^2)_{ij}} + \frac{u-s}{(t-M^2)_{ij}} \right), \end{aligned}$$

where $L_{ij} = g_i g_j \left(\frac{1}{f_i^2} + \frac{1}{f_{i+1}^2} \right) \left(\frac{1}{f_j^2} + \frac{1}{f_{j+1}^2} \right)$.

High energy limit:

$$\mathcal{A}_{W^+ W^- \rightarrow W^+ W^-} \rightarrow -\frac{1}{4} f^4 \sum_{i=1}^{K+1} \frac{u}{f_i^6}$$

minimized when $f_i = f_c, \forall i$:

$$\mathcal{A}_{W^+ W^- \rightarrow W^+ W^-} \rightarrow -\frac{u}{(K+1)^2 v^2}$$

Unitarity condition from $J = 0$ partial wave $|a_0| < 1/2$:

$$a_0 = \frac{s}{16\pi(K+1)^2 v^2} \rightarrow \Lambda = (K+1)1.2 \text{ TeV}$$

Considering all channels: $\Sigma_i = \exp(i\vec{\pi}_i \cdot \vec{\tau}/2f_i)$:

$$\mathcal{A}_{\pi_i \pi_i \rightarrow \pi_i \pi_i} \rightarrow -\frac{1}{4} \frac{u}{f_i^2}$$

The unitarity limit is determined by the smallest f_i . Taking all equal.

$$\Lambda^{TOT} = \sqrt{K+1} 1.2 \text{ TeV}$$

Higgs bosons are not necessary up scales $\sqrt{K+1}$ times the scale of unitarity violation in the Higgsless SM, i.e. 1.2 TeV.

Approximately $M_A^{max} < \Lambda^{TOT}$ implies (when $f_i = f_c$) $g_c \lesssim 5 \Rightarrow \epsilon_3$ too large.

Delocalizing fermion interactions

(Casalbuoni, De Curtis, Dolce, D.; see also Chivukula, Simmons, He, Kurachi)

Let us build

$$\chi_L^i = \Sigma_i^\dagger \Sigma_{i-1}^\dagger \cdots \Sigma_1^\dagger \psi_L, \quad i = 1, \dots, K$$

Transformation properties

$$\chi_L^i \rightarrow U_i \chi_L^i, \quad U_i \in SU(2)_i, \quad i = 1, \dots, K.$$

New invariants:

$$\bar{\chi}_L^i i\gamma^\mu (\partial_\mu + ig_i A_\mu^i + \frac{i}{2} \tilde{g}' (B - L) \tilde{\mathcal{Y}}_\mu) \chi_L^i, \quad i = 1, \dots, K$$

New fermion lagrangian:

$$\begin{aligned} \mathcal{L}_{fermions}^{tot} &= \bar{\psi}_L i\gamma^\mu \left[\partial_\mu + i\tilde{g} \tilde{W}_\mu + \frac{i}{2} \tilde{g}' (B - L) \tilde{\mathcal{Y}}_\mu \right] \psi_L + \\ &+ \sum_{i=1}^K b_i \bar{\chi}_L^i i\gamma^\mu \left[\partial_\mu + ig_i A_\mu^i + \frac{i}{2} \tilde{g}' (B - L) \tilde{\mathcal{Y}}_\mu \right] \chi_L^i + \\ &+ \bar{\psi}_R i\gamma^\mu \left[\partial_\mu + i\tilde{g}' \frac{\tau^3}{2} \tilde{\mathcal{Y}}_\mu + \frac{i}{2} \tilde{g}' (B - L) \tilde{\mathcal{Y}}_\mu \right] \psi_R. \end{aligned}$$

b_i dimensionless parameters. In the unitary gauge ($\Sigma_i \equiv I$) and after a

rescaling $\psi_L \rightarrow \frac{1}{\sqrt{1 + \sum_{i=1}^K b_i}} \psi_L$:

$$\begin{aligned}
 \mathcal{L}_{fermions}^{tot} &= \bar{\psi}_R i\gamma^\mu \left[\partial_\mu + i\tilde{g}' \frac{\tau^3}{2} \tilde{\mathcal{Y}}_\mu + \frac{i}{2} \tilde{g}' (B - L) \tilde{\mathcal{Y}}_\mu \right] \psi_R + \\
 &+ \bar{\psi}_L i\gamma^\mu \left[\partial_\mu + \frac{1}{1 + \sum_{i=1}^K b_i} \left(i\tilde{g} \tilde{W}_\mu + \sum_{i=1}^K b_i i g_i A_\mu^i \right) \right. \\
 &\left. + \frac{i}{2} \tilde{g}' (B - L) \tilde{\mathcal{Y}}_\mu \right] \psi_L.
 \end{aligned}$$

Low-energy limit

Eliminating the A_i fields when $(\tilde{g}/g_i)^2 \ll 1$, $\forall i$ and after a field redefinition:

$$\mathcal{L}_{eff}^{charg} = \frac{-\tilde{e}}{\sqrt{2}\tilde{s}_\theta} \left(1 - \frac{b}{2} - \frac{z_w}{2}\right) \bar{\psi} \gamma^\mu \frac{1 - \gamma_5}{2} \psi W_\mu^- + h.c.,$$

$$\mathcal{L}_{eff}^{neutr} = \frac{-\tilde{e}}{\tilde{s}_\theta \tilde{c}_\theta} \left(1 - \frac{b}{2} - \frac{z_z}{2}\right) \bar{\psi} \gamma^\mu \left[T_L^3 \frac{1 - \gamma_5}{2} - Q \tilde{s}_\theta^2 \frac{1 - \frac{\tilde{c}_\theta}{\tilde{s}_\theta} z_{z\gamma}}{1 - \frac{b}{2}} \right] \psi Z_\mu,$$

$$- \tilde{e} \left(1 - \frac{z_\gamma}{2}\right) \bar{\psi} \gamma^\mu Q \psi A_\mu.$$

where

$$z_\gamma = \tilde{s}_\theta^2 \sum_{i=1}^K \left(\frac{\tilde{g}}{g_i}\right)^2, \quad z_w = \sum_{i=1}^K \left(\frac{\tilde{g}}{g_i}\right)^2 (1 - y_i)^2,$$

$$z_z = \frac{1}{\tilde{c}_\theta^2} \sum_{i=1}^K \left(\frac{\tilde{g}}{g_i}\right)^2 (\tilde{c}_\theta^2 - y_i)^2, \quad z_{z\gamma} = -\frac{\tilde{s}_\theta}{\tilde{c}_\theta} \sum_{i=1}^K \left(\frac{\tilde{g}}{g_i}\right)^2 (\tilde{c}_\theta^2 - y_i),$$

$$b = \frac{2 \sum_{i=1}^K y_i b_i}{1 + \sum_{j=1}^K b_j}.$$

Current current interaction terms are also generated

$$\mathcal{L}_{eff}^{quart} = \beta \sum_{a=1}^3 \left(\bar{\psi}_L \gamma^\mu \frac{\tau^a}{2} \psi_L \right)^2$$

with

$$\beta = \frac{1}{8f^2} (\bar{b}_K - b)^2 - \frac{1}{8f^2} \sum_{i=1}^K x_{i+1} \bar{b}_i^2$$

$x_i = f^2/f_i^2$ and

$$\bar{b}_i = 2 \frac{\sum_{j=1}^i b_j}{1 + \sum_{j=1}^K b_j} \quad (i = 1, \dots, K).$$

Physical quantities:

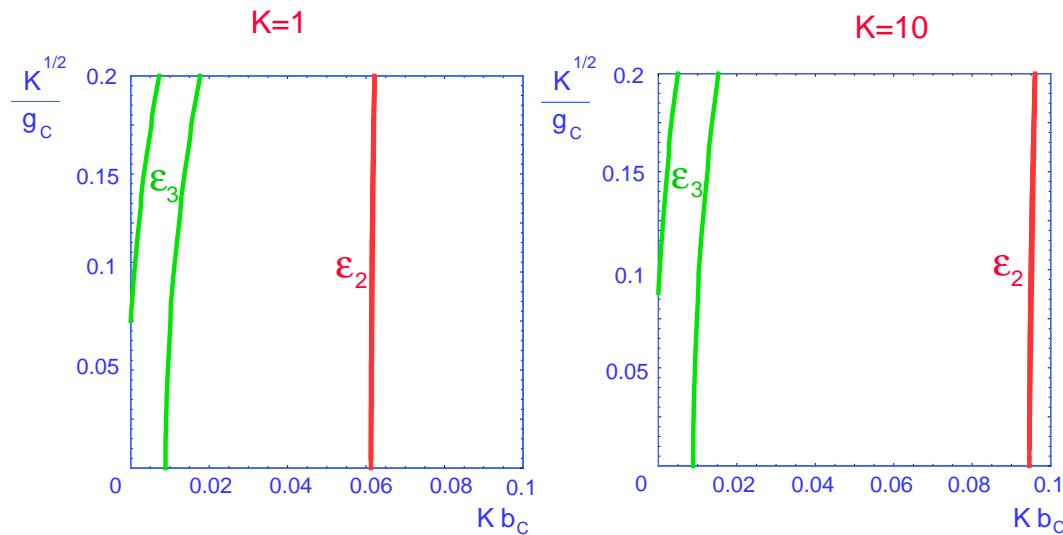
$$M_Z^2 = \tilde{M}_Z^2 (1 - z_z), \quad M_W^2 = \tilde{M}_W^2 (1 - z_w),$$

$$e = \tilde{e} \left(1 - \frac{z_\gamma}{2}\right), \quad \frac{G_F}{\sqrt{2}} = \frac{1}{8} \tilde{g}^2 \left(1 - \frac{b}{2}\right)^2 \frac{1 - z_w}{M_W^2} + \frac{1}{4\beta}.$$

$$\epsilon_1 \simeq 0, \quad \epsilon_2 \simeq 0 \quad \epsilon_3 \simeq \sum_{i=1}^K y_i \left(\frac{\tilde{g}^2}{g_i^2} (1 - y_i) - b_i \right).$$

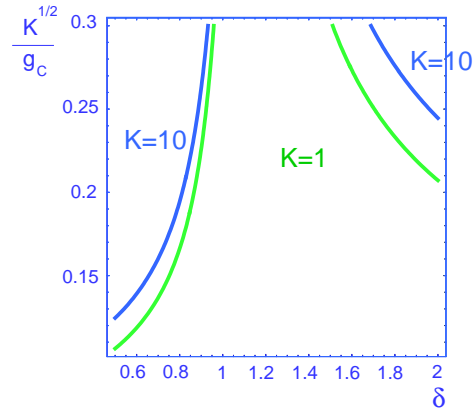
where $y_i = \sum_{j=1}^i \frac{f_j^2}{f_j^2}$. Assume: $g_i \equiv g_c$, $b_i \equiv b_c$, $f_i \equiv f_c$, $\forall i$.

95% CL for ϵ_1 , independent on g_c , $b_c < 0.14$ for $K = 1$, $b_c < 0.025$ for $K = 10$.



95% CL bounds on the parameter space $(Kb_c, \sqrt{K}/g_c)$ from the experimental values of ϵ_2 and ϵ_3 for $K = 1$ (left) $K = 10$ (right). The allowed parameter space from ϵ_2 is the region to the left of the dashed line and from ϵ_3 the region between the continuous lines.

Assuming $b_i = \delta \frac{\tilde{g}^2}{g_i^2} (1 - y_i)$, ($g_i \equiv g_c, f_i \equiv f_c, \forall i$):



95% CL bounds on the parameter space $(\delta, \sqrt{K}/g_c)$ from the experimental value of ϵ_3 for $K = 1$ (continuous line), ($K = 10$ dash line). The allowed parameter space is the region between the corresponding lines.

In conclusion with some fine tuning a portion of parameter space is allowed.

Continuous limit ($K \rightarrow \infty$)

Let $K \rightarrow \infty$ with $Ka \rightarrow \pi R$, R being the length of the segment.

$$\lim_{a \rightarrow 0} a f_i^2 = f^2(y), \quad \lim_{a \rightarrow 0} a g_i^2 = g_5^2(y), \quad \lim_{a \rightarrow 0} \frac{b_i}{a} = b(y).$$

Assuming $g_5(y) = g_5$

$$\epsilon_3 \equiv 0 \rightarrow b(y) = \frac{\tilde{g}^2}{g_5^2} \int_y^{\pi R} dt \frac{f^2}{f^2(t)}, \quad \frac{1}{f^2} = \int_0^{\pi R} \frac{dy}{f^2(y)}.$$

Flat metric $f(y) = \bar{f}$

$$b(y) = \frac{\tilde{g}^2}{g_5^2} \left(1 - \frac{y}{\pi R} \right).$$

Randall-Sundrum metric $f(y) = \bar{f} e^{ky}$

$$b(y) = \frac{\tilde{g}^2}{g_5^2} \frac{e^{-2\pi k R} - e^{-2ky}}{e^{-2\pi k R} - 1}.$$

In general: $b(0) = \frac{\tilde{g}^2}{g_5^2}$, $b(\pi R) = 0$.

$$\Sigma^j = e^{i \int_{y_j}^{y_j+a} dz A_5(z, x_\mu)} \quad : \quad \Sigma_1 \cdots \Sigma_i \rightarrow P \left[\exp(i \int_0^y dz A_5(z, x_\mu)) \right]$$

$$\chi_L^i(x_\mu) = \Sigma_i^\dagger \cdots \Sigma_1^\dagger \psi_L(x_\mu) \quad \rightarrow \quad \chi_L(y, x_\mu) = P \left[\exp(i \int_0^y dz A_5(z, x_\mu)) \right]^\dagger \psi_L(x_\mu)$$

Fermions leave on the branes but interact with bulk gauge bosons via Wilson lines.

Mass terms for the fermions

$$\lambda^{ij} \bar{\psi}_L^i \Sigma_1 \Sigma_2 \cdots \Sigma_{K+1} \psi_R^j \rightarrow \lambda^{ij} \bar{\psi}_L^i P \left[\exp(i \int_0^{\pi R} dz A_5(z, x_\mu)) \right] \psi_R^j.$$

Conclusions

- **Moose models appear deconstructing Higgsless models from five to four dimensions**
- **Hope: the scale where partial wave unitarity is violated is higher w.r.t. the Higgsless SM due to the exchange of KK excitations in the four gauge boson amplitude scattering**
- **Problem: compatibility between precision electroweak data and unitarity requirement**
- **Possible solution with fine tuning: delocalize the fermion interactions**
- **Signature: new gauge bosons at future colliders (Birkedal, Matchev, Perelstein)**