

# Neutralino Annihilation into Photons:

$$\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow \gamma\gamma$$

$$\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow Z\gamma$$

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# Motivation

- **Neutralino: a natural candidate to Dark Matter within the MSSM**
- **Astrophysical experiments performing direct and indirect searches**
  - Ground based: Cangaroo, HESS, MAGIC, VERITAS ...
  - Space telescopes: EGRET, AMS, GLAST ...
- **Indirect searches: looking for products of  $\tilde{\chi}_1^0$  annihilation**
  - Photons point back the source
  - Charged particles suffer propagation uncertainties
- **“Direct” photon production gives a clear signal**
  - Energy spectrum peak at  $M_{\tilde{\chi}_1^0}$
  - No astrophysical background
- **First application of a code computing one-loop processes in the MSSM**
  - Collider Physics
  - Astrophysical/relic density calculations

# Particle Physics Content

( $\gamma\gamma$ : Bergström, Ullio'97, Bern, Gondolo'97)  
( $Z\gamma$ : Ullio, Bergström'97)

The gamma ray flux is

$$\Gamma_\gamma(\psi) \propto \frac{\sigma v}{M_{\tilde{\chi}_1^0}^2} \int_{l.o.s} \rho^2(l) dl(\psi)$$

where  $\rho$  is the neutralino density  
 $\psi$  is the observation-galactic centre angle

## • Particle physics:

we compute the MSSM one-loop cross-sections:

$$\begin{aligned} \tilde{\chi}_1^0 \tilde{\chi}_1^0 &\rightarrow \gamma\gamma \\ \tilde{\chi}_1^0 \tilde{\chi}_1^0 &\rightarrow Z\gamma \end{aligned}$$

First results of a SUSY one-loop code

## • Astrophysics content:

to be implemented in micrOMEGAs

# A very special computational strategy

**Lagrangian of the model  
defined in LanHEP**

- particle content
- interaction terms
- shifts in fields and parameters
- ghost terms constructed by BRST



**Generic Model**  
-kinematical structures



**Classes Model**  
-Feynman rules, including CT



**Evaluation via  
FeynArts-FormCalc**

**LoopTools modified!!**



**Renormalisation scheme**

- definition of renorm. const. in the classes model

# Very powerful tool

→ Flexibility of the code allows

- Physics beyond the MSSM: Split SUSY, Majorana Neutrinos, NMSSM
- Different renormalisation schemes:  $\tan\beta$  problem

→ Tests on the results

- IR and UV finiteness: dependence on  $C_{UV} = \frac{1}{\epsilon} - \gamma_E + \log 4\pi$  and  $m_\gamma$
- Gauge invariance: Non-linear gauge

$$\mathcal{L}_{GF} = -\frac{1}{\xi_W} |(\partial_\mu - ie\tilde{\alpha}\gamma_\mu - igc_W\tilde{\beta}Z_\mu)W^{\mu+} + \xi_W\frac{g}{2}(v + \tilde{\delta}h_o + \tilde{\omega}H_o + i\tilde{\kappa}\chi_3)\chi^+|^2 \\ -\frac{1}{2\xi_Z}(\partial.Z + \xi_Z\frac{g}{2c_W}(v + \tilde{\epsilon}h_o + \tilde{\gamma}H_o)\chi_3)^2 - \frac{1}{2\xi_\gamma}(\partial.\gamma)^2$$

$\xi = 1 \rightarrow$  no high order tensor analysis  
proper choice for gauge parameters simplifies computation

## Tested for the SM

# LoopTools Modified!

Routine computing loop integrals

If both  $\chi$  are at rest ( $v = 0$ ) the kinematic is very special

General case:  $p_\chi^{(1)} + p_\chi^{(2)} = p_\gamma + p_Z$

In this case:  $p_\chi^{(1)} \simeq p_\chi^{(2)}$  so just two independent momentum

Tensor integrals reduction requires inverse Gram determinant computation

$$\det \begin{bmatrix} p_1^2 & p_1 p_2 & p_1 p_3 \\ p_1 p_2 & p_2^2 & p_2 p_3 \\ p_1 p_3 & p_2 p_3 & p_3^2 \end{bmatrix} \propto v^2$$

in our case  $v/c \simeq 10^{-3}$  giving numerical instabilities

To solve this problem we implement the

**Segmentation of one-loop integrals at  $v = 0$**

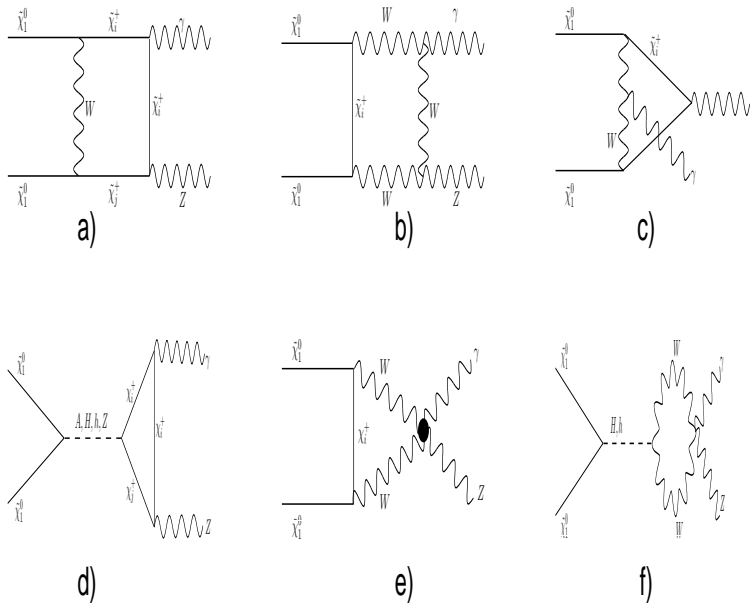
N-points integrals  $\rightarrow$  (N-1) integrals

$$\frac{1}{D_0 D_1 D_2 D_3} \propto \frac{1}{D_0 D_1 D_2} + \frac{a}{D_0 D_1 D_3} + \frac{b}{D_0 D_2 D_3} - \frac{1+a+b}{D_1 D_2 D_3}$$

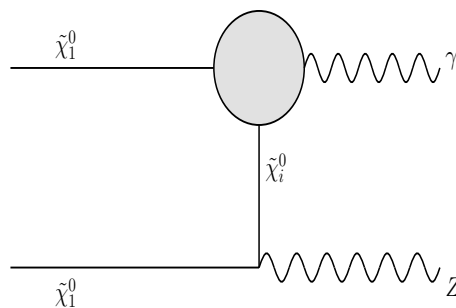
$$D_0 = k^2 - m_0^2, D_i = (k + p_i)^2 - m_i^2$$

# Computing the cross-sections

More than a thousand diagrams including



New contribution found in  $Z\gamma$  !



Counterterm contribution:

- Obtained from tree-level  $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow ZZ$  and  $\delta Z_{Z\gamma}$
- Since  $\delta Z_{Z\gamma} \sim (1 - \tilde{\alpha})$  CT can be put to zero if  $\tilde{\alpha} = 1$

Choosing a proper gauge simplifies the computation

# Numerical results

DarkSUSY: Gondolo et al. [www.physto.se/edsjo/darksusy](http://www.physto.se/edsjo/darksusy)

PLATON: Gounaris et al. [dtp.physics.auth.gr/platon](http://dtp.physics.auth.gr/platon)

|  | Sugra                | nSugra               | higgsino-1           | higgsino-2           | wino-1               | wino-2               |
|--|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| $M_1$                                    | 0.2                  | 0.1                  | 0.5                  | 20.                  | 0.5                  | 20.0                 |
| $M_2$                                    | 0.4                  | 0.4                  | 1.0                  | 40.                  | 0.2                  | 4.0                  |
| $\mu$                                    | 1.0                  | 1.0                  | 0.2                  | 4.0                  | 1.0                  | 40.0                 |
| $M_A$                                    | 1.0                  | 1.0                  | 1.0                  | 10.                  | 1.0                  | 10.0                 |
| $m_{\tilde{f}}$                          | 0.8                  | 0.8                  | 0.8                  | 10.                  | 0.8                  | 10.0                 |
| $\Omega h^2$                             | 5.31                 | 18.8                 | $6.41 \cdot 10^{-3}$ | 1.59                 | $1.16 \cdot 10^{-3}$ | 0.46                 |
| $\sigma v_{\gamma\gamma} \times 10^{27}$ |                      |                      |                      |                      |                      |                      |
| v=0                                      | $5.82 \cdot 10^{-5}$ | $1.58 \cdot 10^{-5}$ | $7.01 \cdot 10^{-2}$ | $4.71 \cdot 10^{-2}$ | 1.99                 | 1.52                 |
| PLATONdm1                                | $5.82 \cdot 10^{-5}$ | $1.58 \cdot 10^{-5}$ | $7.01 \cdot 10^{-2}$ | $4.72 \cdot 10^{-2}$ | 1.99                 | 1.53                 |
| DarkSUSY                                 | $5.81 \cdot 10^{-5}$ | $1.58 \cdot 10^{-5}$ | $7.02 \cdot 10^{-2}$ | $4.71 \cdot 10^{-2}$ | 1.99                 | 1.52                 |
| v=0.5                                    | $5.94 \cdot 10^{-5}$ | $1.60 \cdot 10^{-5}$ | $1.30 \cdot 10^{-1}$ | $5.42 \cdot 10^{-3}$ | 2.36                 | $8.69 \cdot 10^{-2}$ |
| $\sigma v_{gg} \times 10^{30}$           |                      |                      |                      |                      |                      |                      |
| v=0                                      | 2.05                 | 0.60                 | 5.74                 | 0.33                 | 19.6                 | 0.42                 |
| PLATONdmg                                | 2.05                 | 0.60                 | 5.75                 | 0.33                 | 19.6                 | 0.42                 |
| DarkSUSY                                 | 2.05                 | 0.60                 | 5.77                 | 0.33                 | 19.5                 | 0.42                 |
| v=0.5                                    | 2.21                 | 0.60                 | 8.23                 | 0.33                 | 20.2                 | 0.42                 |
| PLATONgrel                               | 2.21                 | 0.60                 | 8.23                 | 0.33                 | 20.2                 | 0.42                 |
| $\sigma v_{Z\gamma} \times 10^{27}$      |                      |                      |                      |                      |                      |                      |
| v=0,full                                 | $2.03 \cdot 10^{-5}$ | $2.61 \cdot 10^{-6}$ | $2.19 \cdot 10^{-1}$ | $2.20 \cdot 10^{-2}$ | 11.7                 | 10.1                 |
| v=0,part                                 | $1.94 \cdot 10^{-5}$ | $2.50 \cdot 10^{-6}$ | $2.61 \cdot 10^{-1}$ | $3.29 \cdot 10^{-2}$ | 11.7                 | 10.1                 |
| DarkSUSY                                 | $1.42 \cdot 10^{-5}$ | $1.79 \cdot 10^{-6}$ | $2.61 \cdot 10^{-1}$ | $3.29 \cdot 10^{-2}$ | 11.7                 | 10.1                 |
| v=0.5,full                               | $2.45 \cdot 10^{-5}$ | $3.67 \cdot 10^{-6}$ | $2.99 \cdot 10^{-1}$ | $1.66 \cdot 10^{-2}$ | 14.2                 | $5.76 \cdot 10^{-1}$ |
| v=0.5,part                               | $2.34 \cdot 10^{-5}$ | $3.53 \cdot 10^{-6}$ | $3.58 \cdot 10^{-1}$ | $2.47 \cdot 10^{-1}$ | 14.2                 | $5.76 \cdot 10^{-1}$ |

$\tan \beta = 10$ ,  $A = 0$  but  $A_t = -0.3$  when  $m_{\tilde{f}} = 0.8$ , all in TeV

Large cross-sections for  $\tilde{\chi}_1^0$  mostly wino or higgsino

Good agreement for  $\gamma\gamma$ ,  $gg$  and relevant  $Z\gamma$

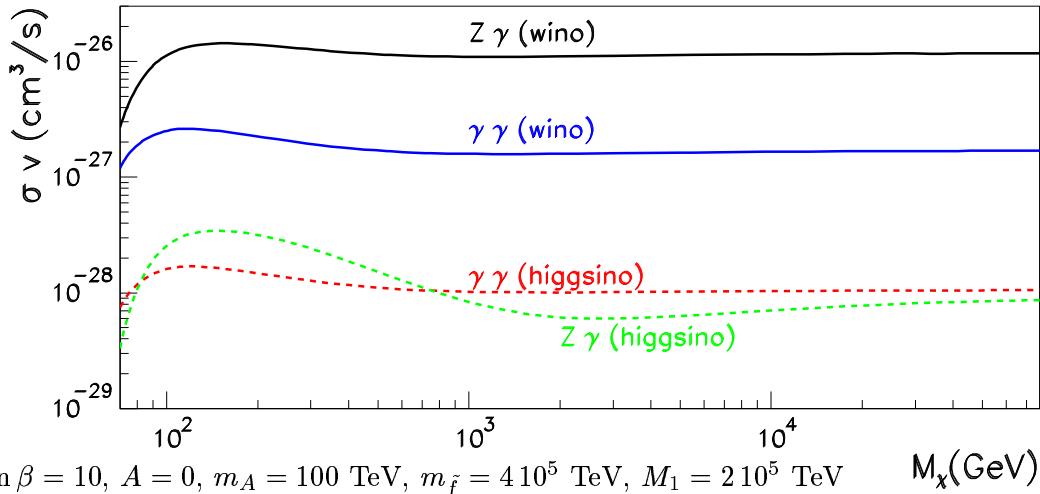
Large new contribution effects in the higgsino case

New  $v = 0.5$  results for  $\gamma\gamma$ ,  $Z\gamma$



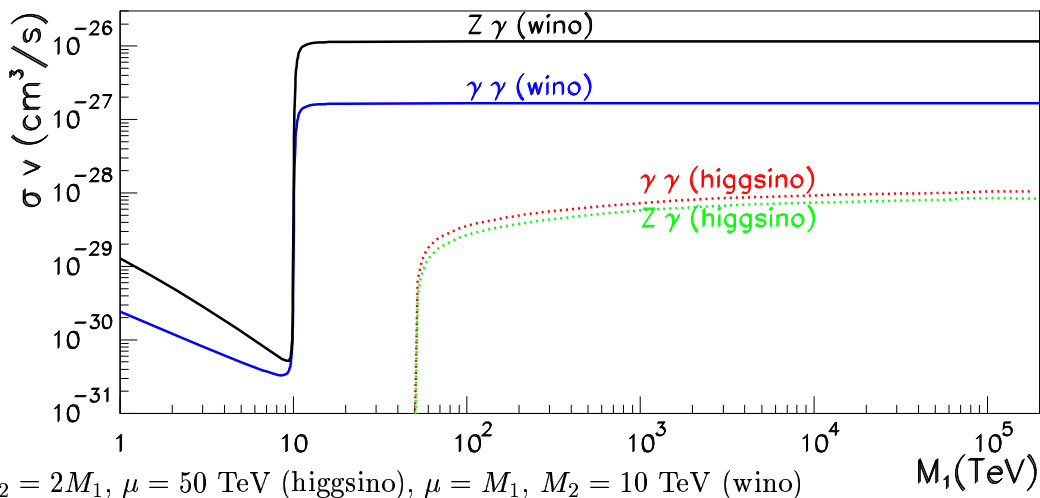
# Higgsino and Wino limits

- $\sigma v$  vs.  $M_{\tilde{\chi}_1^0}$  ( $v = 0$ )



$\tan \beta = 10$ ,  $A = 0$ ,  $m_A = 100$  TeV,  $m_{\tilde{f}} = 4 \cdot 10^5$  TeV,  $M_1 = 2 \cdot 10^5$  TeV  
 $M_2 = 2M_1$  (higgsino),  $\mu = M_1$  (wino)

- $\sigma v$  vs. % higgsino/wino ( $v = 0$ )



$M_2 = 2M_1$ ,  $\mu = 50$  TeV (higgsino),  $\mu = M_1$ ,  $M_2 = 10$  TeV (wino)

$$\delta M = M_{\tilde{\chi}_1^+} - M_{\tilde{\chi}_1^0}$$

Asymptotic value for large  $M_{\tilde{\chi}_1^0}$ ,  $\sigma v \sim 1/M_W^2$

Largest cross section for  $Z\gamma$  in wino case

Smooth behaviour in higgsino case,  $\delta M \sim m_z^2/M_1$

Constant value after transition in wino case,  $\delta M \sim m_z^4/M_1^3$

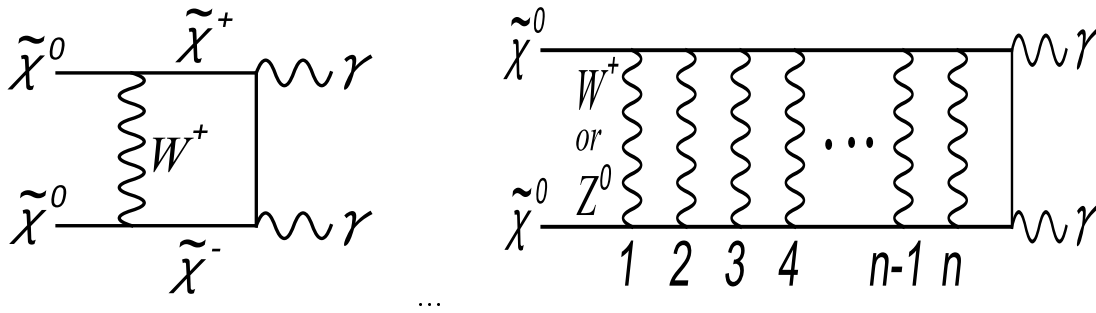
Numerical results reproduce analytical behaviour

# Matching with non-perturbative computation

Hisano et al.'04

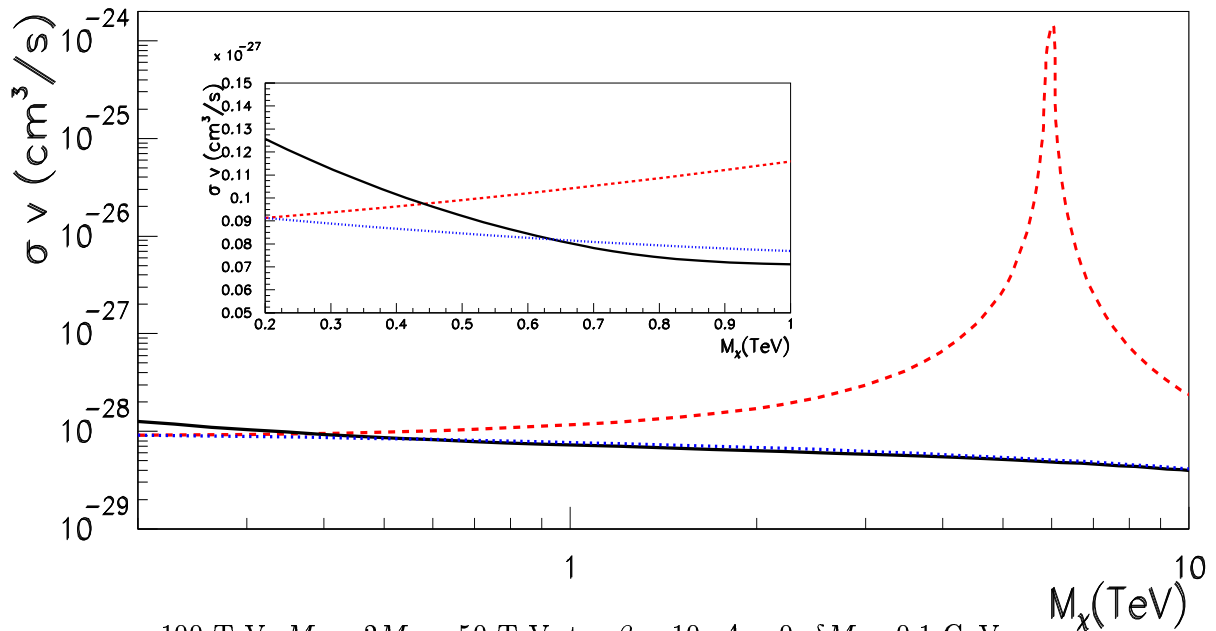
In the extreme higgsino and wino limits,

- one-loop treatment breaks unitarity
- non-perturbative non-relativistic approach



## Non-perturbative computation and one-loop results

higgsino case ( $v = 0$ )



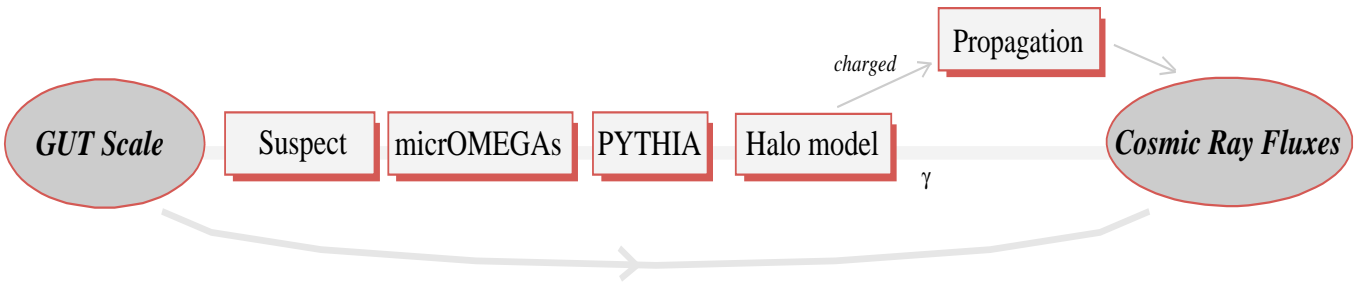
$m_{\tilde{f}} = m_A = 100$  TeV,  $M_2 = 2M_1 = 50$  TeV,  $\tan \beta = 10$ ,  $A = 0$ ,  $\delta M = 0.1$  GeV

Resonances can enhance result several orders of magnitude  
 Matching will take place around 400 – 500 GeV

# Indirect Dark Matter searches

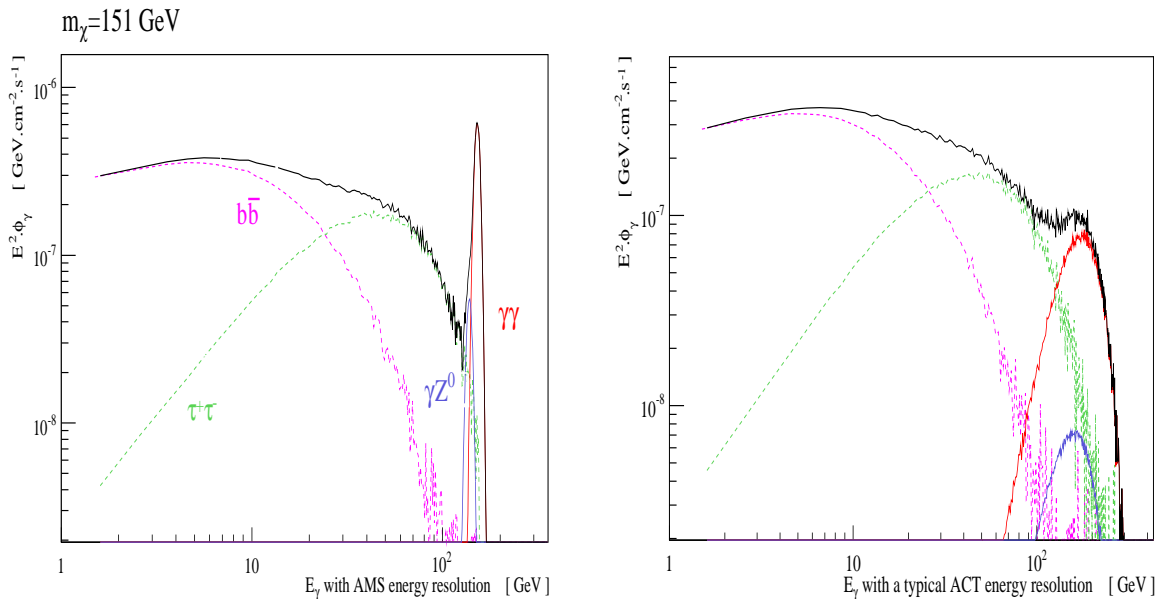
micrOMEGAs  
Brun, Rosier-Lees'05 (AMS/HESS Coll.)

micrOMEGAs will perform indirect  $\tilde{\chi}_1^0$  searches



First analysis, including our code for  $\gamma\gamma, Z\gamma$

just Susy signals are shown  
acceptance is not included



NFW halo param.  $(\alpha, \beta, \gamma) = (1, 3, 1)$ ,  $a = 25$  kpc. (core radius),  $r_0 = 8$  kpc (galactic centre distance),  
 $\rho_0 = 0.3$  GeV/cm<sup>3</sup> (DM density), opening angle cone 1°  
 $m_0 = 113$  GeV,  $m_{1/2} = 375$  GeV,  $A = 0$ ,  $\tan \beta = 20$ ,  $\mu > 0$

$\gamma$  lines could be distinguished from diffuse background

# Conclusions

- **New powerful code** computing one-loop MSSM processes
  - Gauge invariance
  - Different renormalisation schemes
- **Astro/relic density and collider physics**, allows combined LC-LHC-Cosmology analysis
  - Integrals routine improved
- **First results** concerning indirect dark matter searches
  - $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow \gamma\gamma (Z\gamma)$ 
    - Finiteness and gauge invariance checked
    - Good agreement with previous calculations
    - Higgsino and wino limits studied in detail
    - First results given for  $v \neq 0$
    - Matching with non-perturbative calculations analysed
- Code being implemented with micrOMEGAs to perform indirect neutralino searches

Very promising results up to now



a lot of work to do!